

```
(*Problem 1.*)
ClearAll["Global`*"]
```

```
In[25]:= (*1*)
edgeList = {1 ↔ 2, 2 ↔ 3, 2 ↔ 4, 3 ↔ 1, 3 ↔ 2, 4 ↔ 1, 6 ↔ 1, 6 ↔ 3};
```

```
In[26]:= (*2*)
A = 
$$\begin{pmatrix} 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 1 & 0 & 0 \\ 1 & 1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 1 & 0 & 0 & 0 \end{pmatrix};$$

```

```
In[37]:= (*3*)
SparseArray[A] // InputForm
```

```
Out[37]/InputForm=
SparseArray[Automatic, {6, 6}, 0, {1, {{0, 1, 3, 5, 6, 6, 8}}, {{2}, {3}, {4}, {1}, {2}, {1}, {3}}}, {1, 1, 1, 1, 1, 1, 1, 1, 1}}]
```

```
In[38]:= (*4*)
edgeList = edgeList /. (DirectedEdge → UndirectedEdge)
A + AT // MatrixForm
```

```
Out[38]= {1 ↔ 2, 2 ↔ 3, 2 ↔ 4, 3 ↔ 1, 3 ↔ 2, 4 ↔ 1, 6 ↔ 1, 6 ↔ 3}
```

```
Out[39]/MatrixForm=

$$\begin{pmatrix} 0 & 1 & 1 & 1 & 0 & 1 \\ 1 & 0 & 2 & 1 & 0 & 0 \\ 1 & 2 & 0 & 0 & 0 & 1 \\ 1 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 1 & 0 & 0 & 0 \end{pmatrix}$$

```

```
In[40]:= LocalClusteringCoefficient[AdjacencyGraph[A + AT]]
MeanClusteringCoefficient[AdjacencyGraph[A + AT]]
```

```
Out[40]=  $\left\{\frac{1}{2}, \frac{2}{3}, \frac{2}{3}, 1, 0, 1\right\}$ 
```

```
Out[41]=  $\frac{23}{36}$ 
```

```
In[35]:= (*5*)
edgeList /. {5 :-> 6, 6 :-> 5}

$$\begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 1 & 0 \end{pmatrix} \cdot (A + A^T) \cdot \begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 1 & 0 \end{pmatrix} // \text{MatrixForm}$$

```

```
Out[35]= {1 ↔ 2, 2 ↔ 3, 2 ↔ 4, 3 ↔ 1, 3 ↔ 2, 4 ↔ 1, 5 ↔ 1, 5 ↔ 3}
```

```
Out[36]//MatrixForm=
```

$$\begin{pmatrix} 0 & 1 & 1 & 1 & 1 & 0 \\ 1 & 0 & 2 & 1 & 0 & 0 \\ 1 & 2 & 0 & 0 & 1 & 0 \\ 1 & 1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

It cannot be inferred from the edge list how many vertices are isolated.