

DEPENDENCY NETWORK AND NODE INFLUENCE: OVERVIEW AND APPLICATIONS

Dror Y. Kenett

Department of Physics, Boston University, USA

Outline

(1) Introduction to network science

- Terminology
- Network properties
- Matrix representation

(2) Correlation based networks

- Estimating correlations from time series
- Partial correlations
- Dependency network
- Node influence
- Applications in financial markets
- Applications in other systems

(3) Node influence

- I. Cascading failures in industry networks
- II. Overlapping communities in networks
- III. Failure and recovery in networks
- IV. Evolution of networks
- V. Cascading failures in the financial system
- VI. Interdependent networks

(4) Discussion

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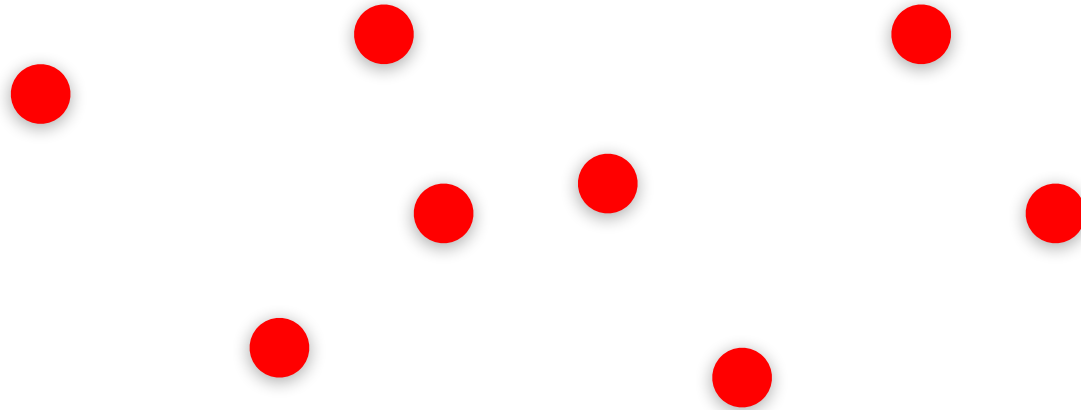
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(4) Discussion

What is a network?

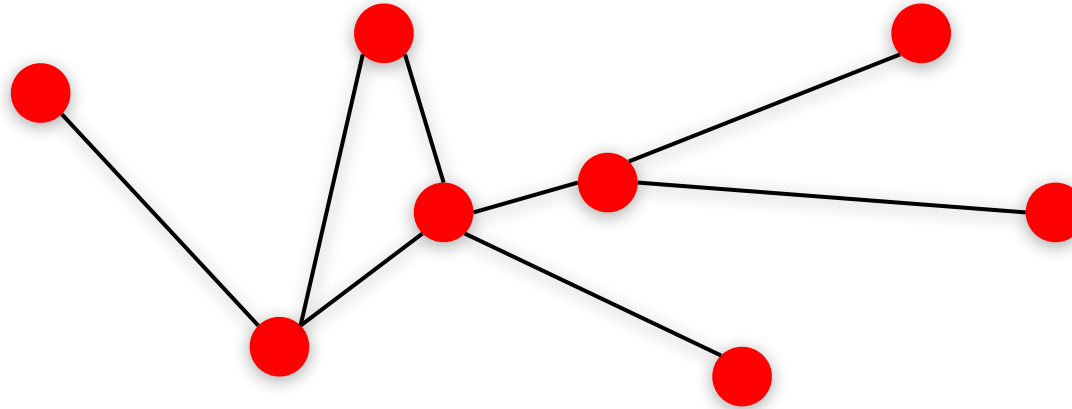
What is a network?



▪ **components:** nodes, vertices

N

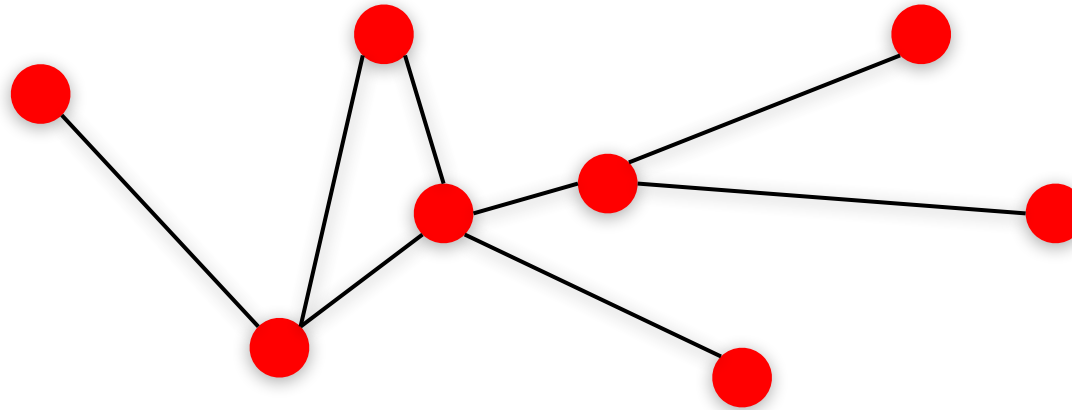
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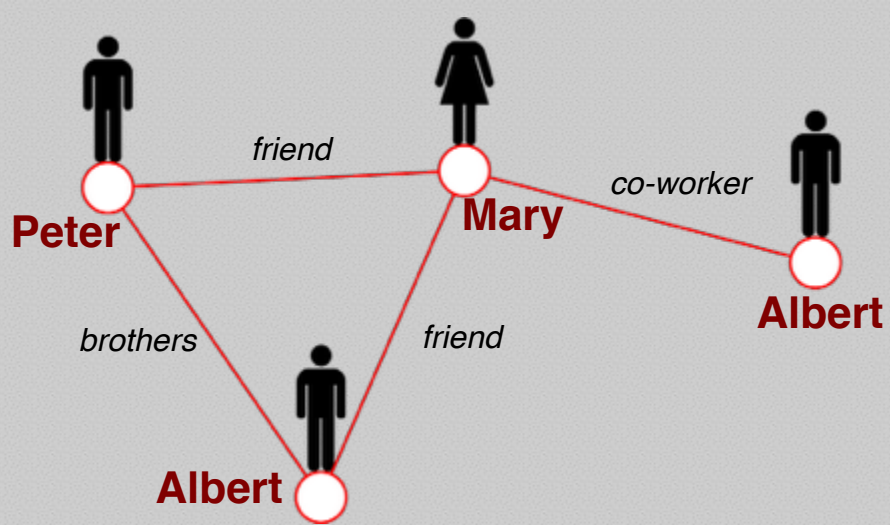
▪ **interactions:** links, edges L

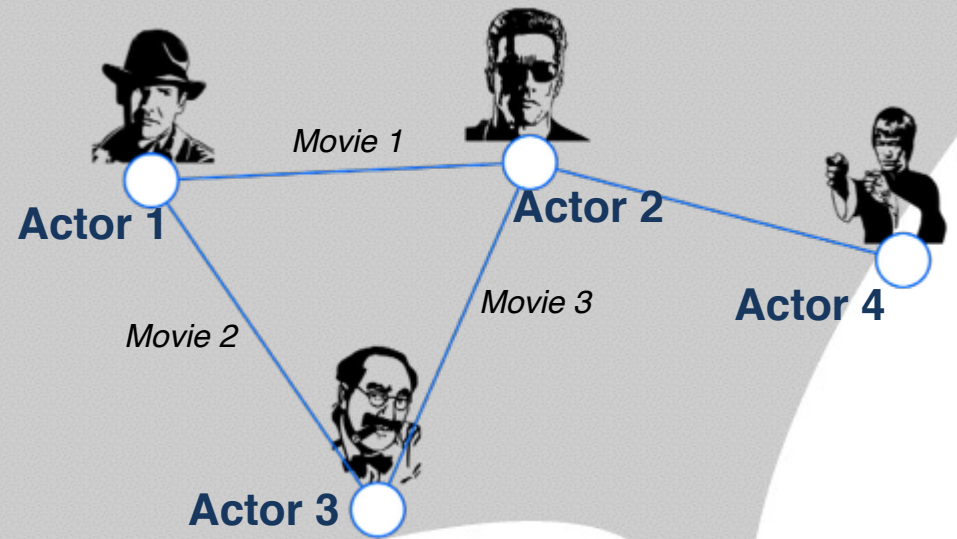
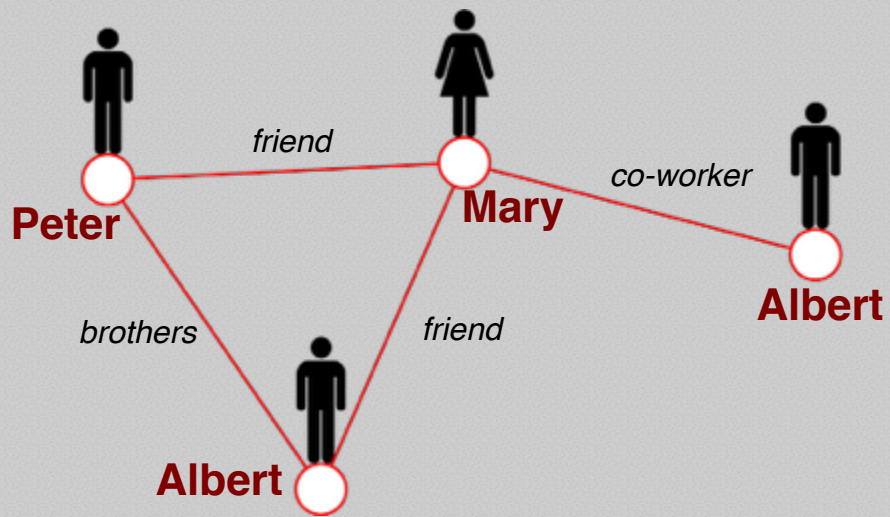
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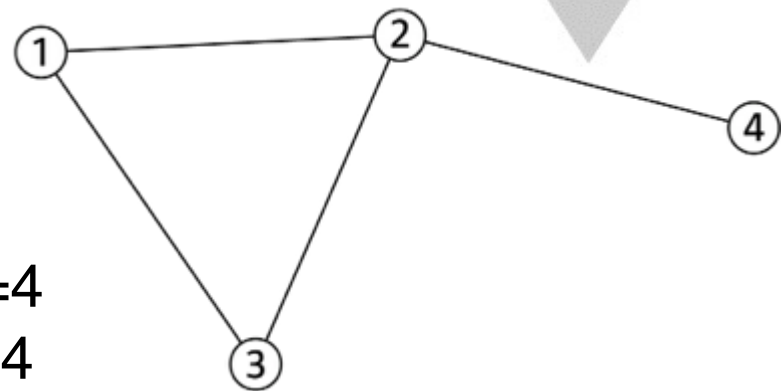
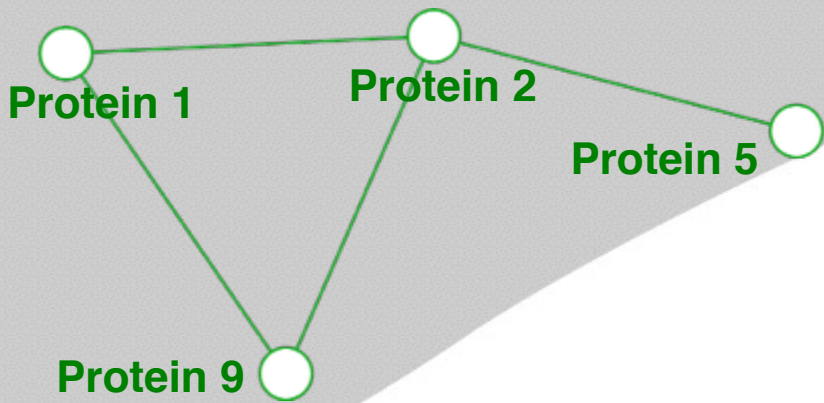
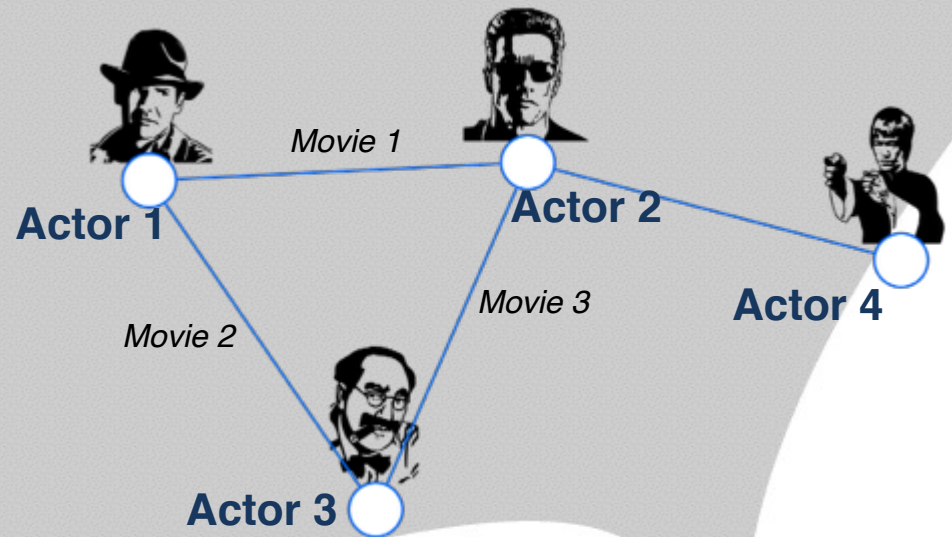
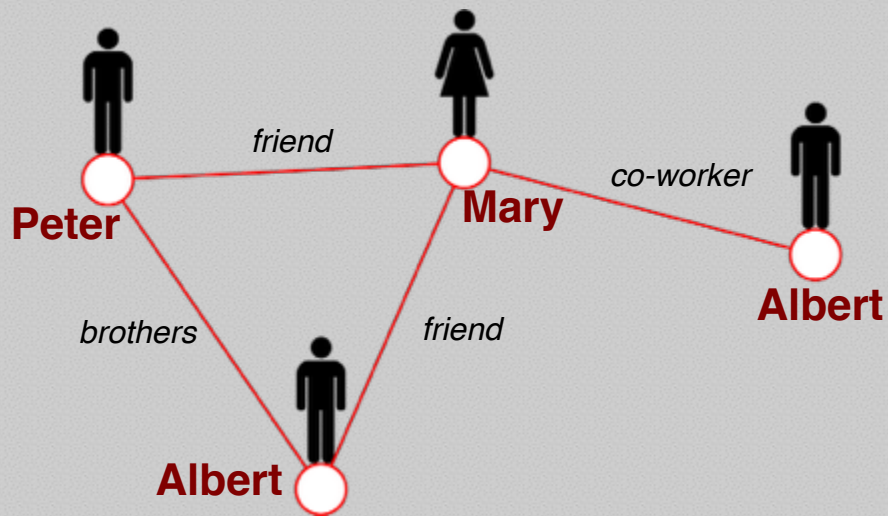


- **components:** nodes, vertices N
- **interactions:** links, edges L
- **system:** network, graph (N,L)









$N=4$
 $L=4$

Network representation?

The choice of the proper network representation determines our ability to use network theory successfully.

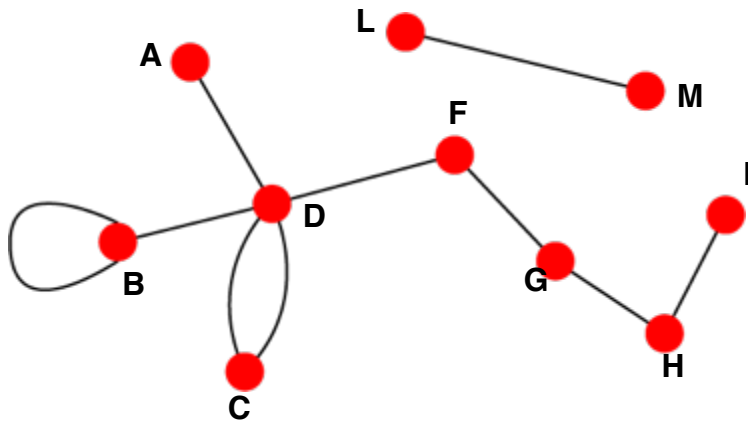
In some cases there is a unique, unambiguous representation. In other cases, the representation is by no means unique.

For example,, the way we assign the links between a group of individuals will determine the nature of the question we can study.

Undirected

Links: undirected (*symmetrical*)

Graph:



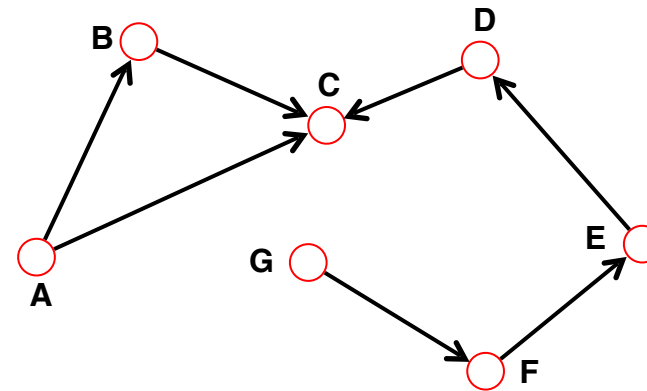
Undirected links :

coauthorship links
Actor network
protein interactions

Directed

Links: directed (*arcs*)

Digraph = directed graph:



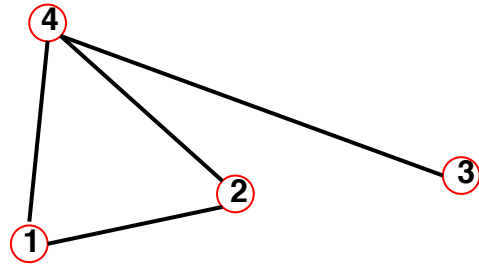
An undirected link is the superposition of two opposite directed links.

Directed links :

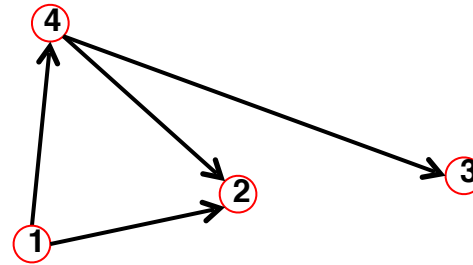
URLs on the www
phone calls
metabolic reactions

The Adjacency Matrix

Undirected



Directed



$A_{ij}=1$ if there is a link between node i and j

$A_{ij}=0$ if nodes i and j are not connected to each other.

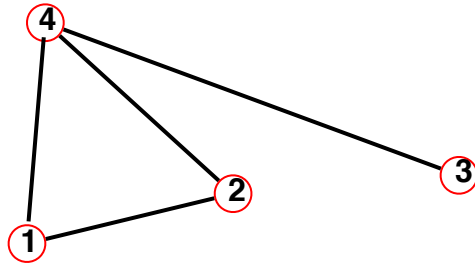
$$A_{ij} = \begin{pmatrix} 0 & 1 & 0 & 1 \\ 1 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \\ 1 & 1 & 1 & 0 \end{pmatrix}$$

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Note that for a directed graph (right) the matrix is not symmetric.

Example of topological properties of a network: Node Degree

Undirected



$$A_{ij} = A_{ji}$$

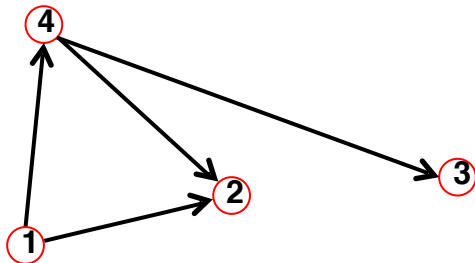
$$A_{ii} = 0$$

$$k_i = \sum_{j=1}^N A_{ij}$$

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$$L = \frac{1}{2} \sum_{i=1}^N k_i = \frac{1}{2} \sum_{ij} A_{ij}$$

Directed



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$$A_{ij} \neq A_{ji}$$

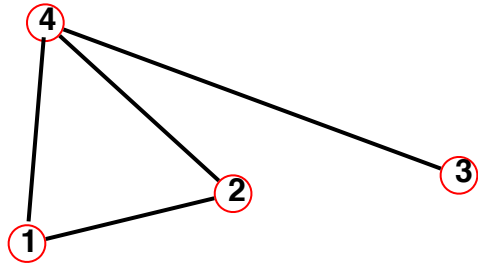
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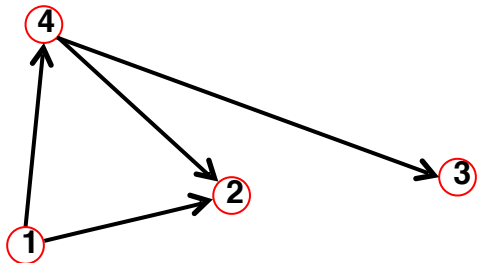
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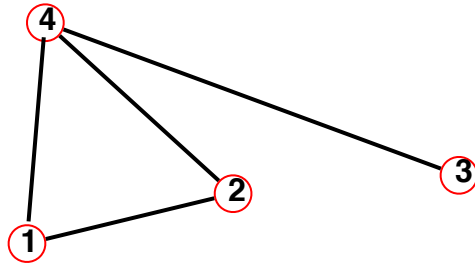
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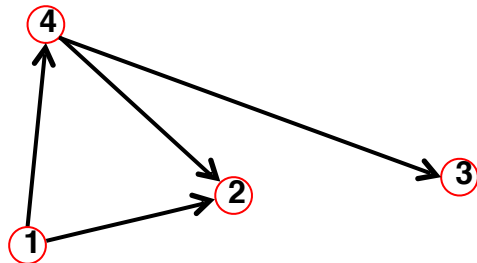
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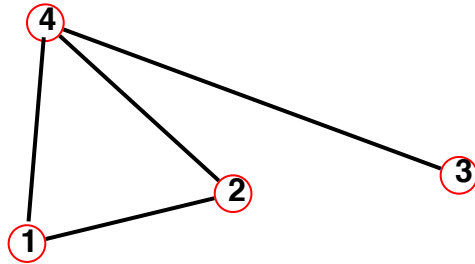
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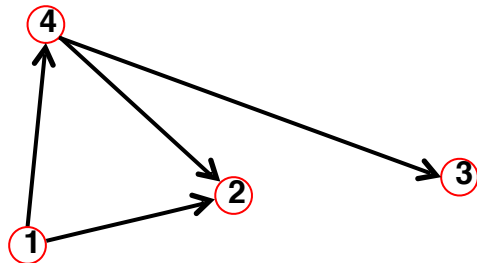
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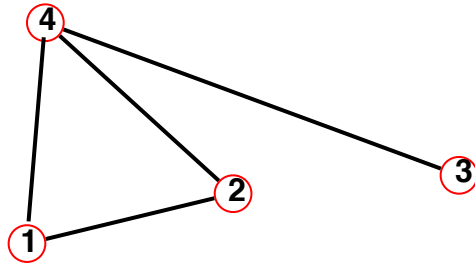
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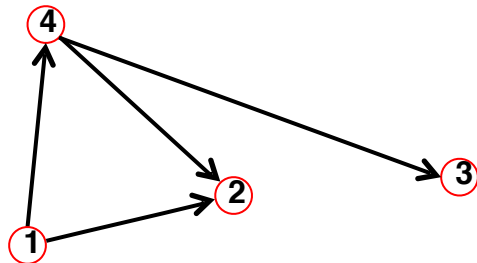
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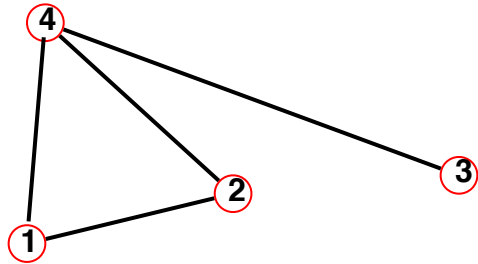
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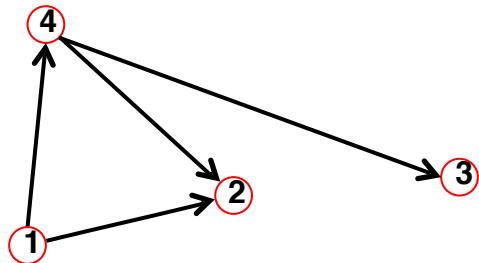
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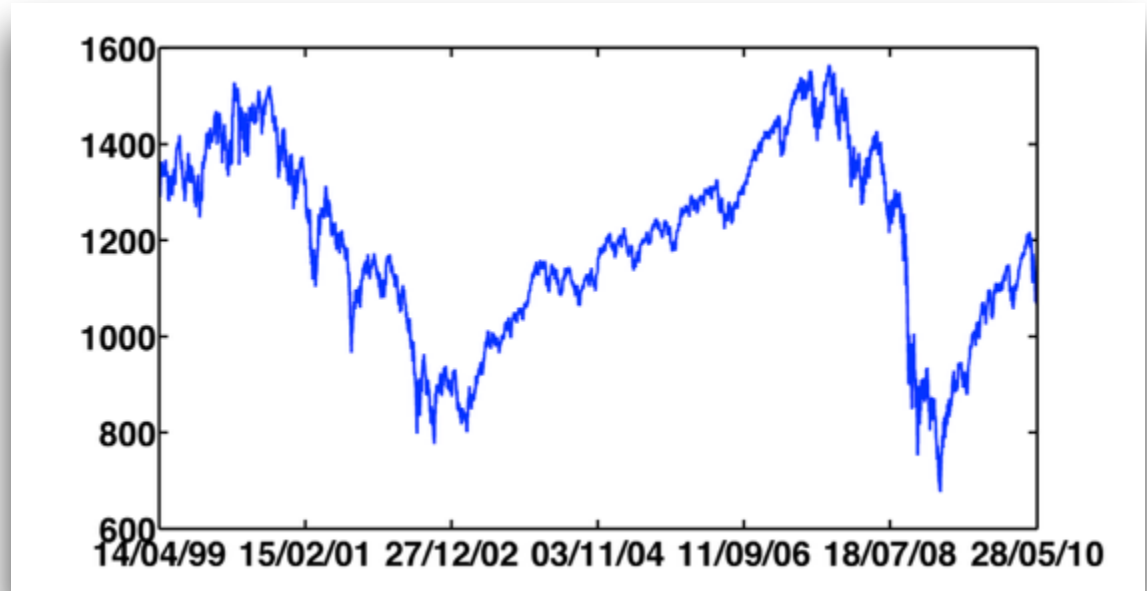
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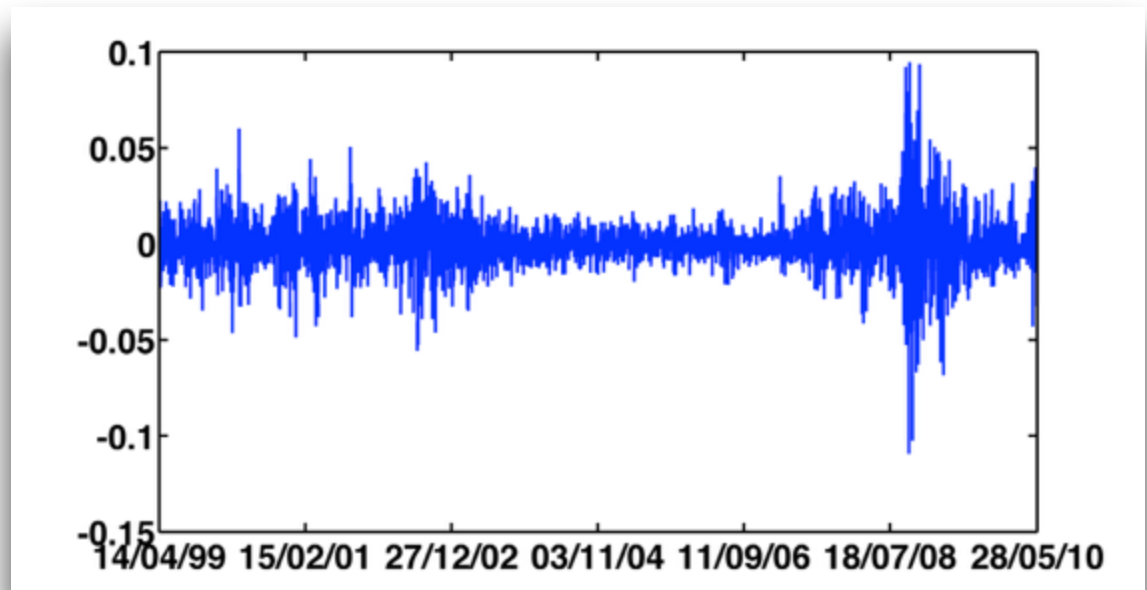
(4) Discussion

S&P500 Price



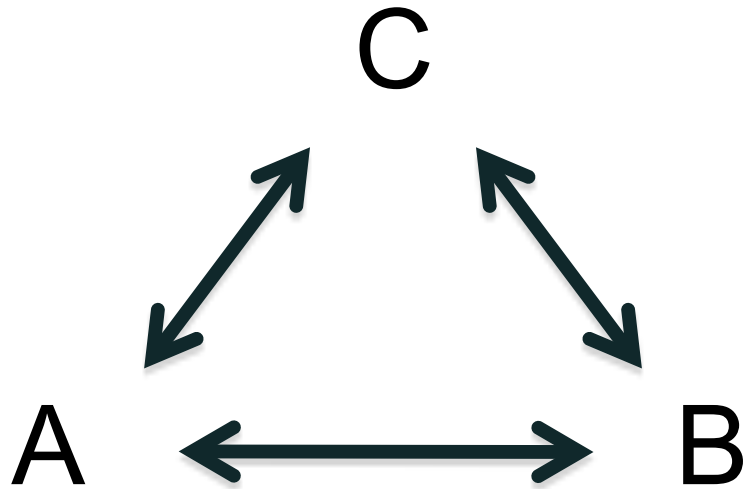
$$r_i(t) = \log [P_i(t)] - \log [P_i(t - 1)]$$

S&P500 Return



Quantifying functional relationships

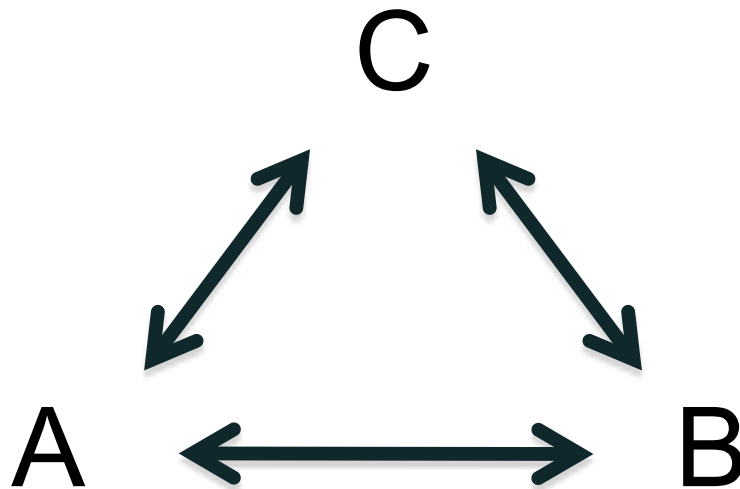
Correlation



$$C(i, j) = \frac{\langle (r_i - \langle r_i \rangle) \cdot (r_j - \langle r_j \rangle) \rangle}{\sigma_i \cdot \sigma_j}$$

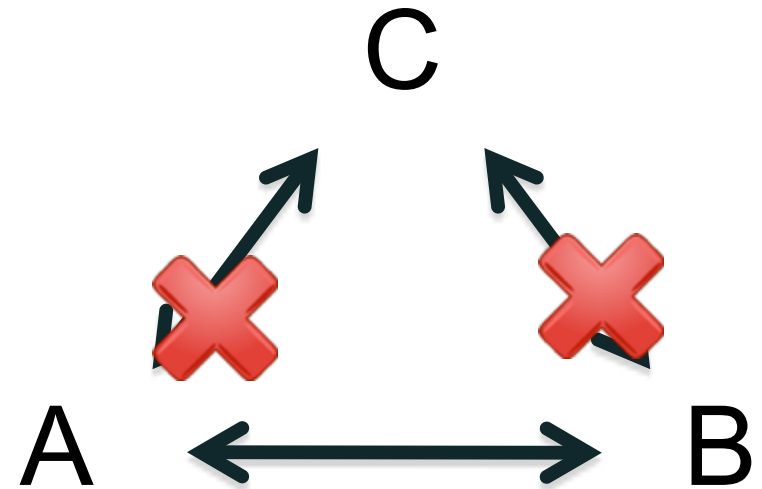
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Partial Correlation



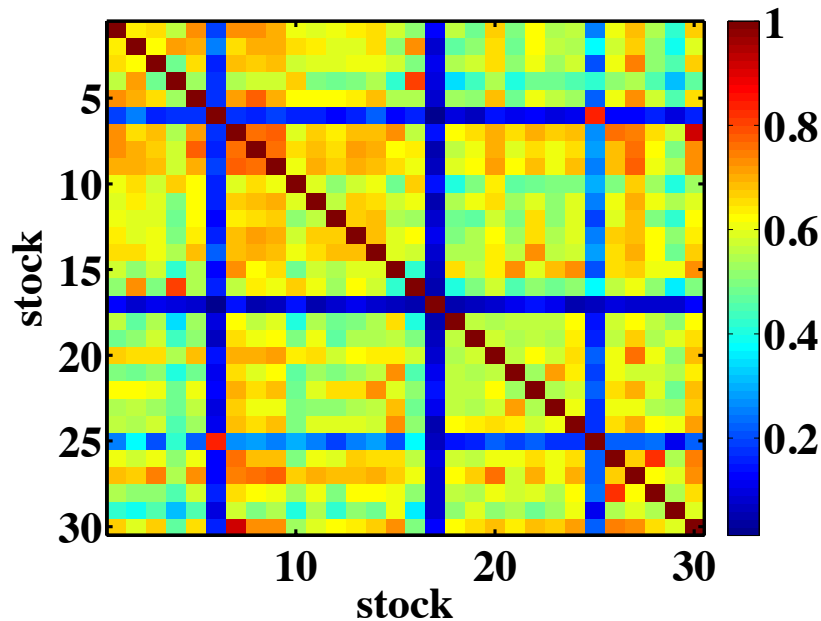
$$PC(i, j | m) = \frac{C(i, j) - C(i, m) \cdot C(j, m)}{\sqrt{(1 - C^2(i, m)) \cdot (1 - C^2(j, m))}}$$

PARTIAL CORRELATION:

The partial correlation (residual correlation) between i and j given m , is the correlation between i and j after removing their dependency on m ; thus, it is a measure of the correlation between i and j after removing the affect of m on their correlation

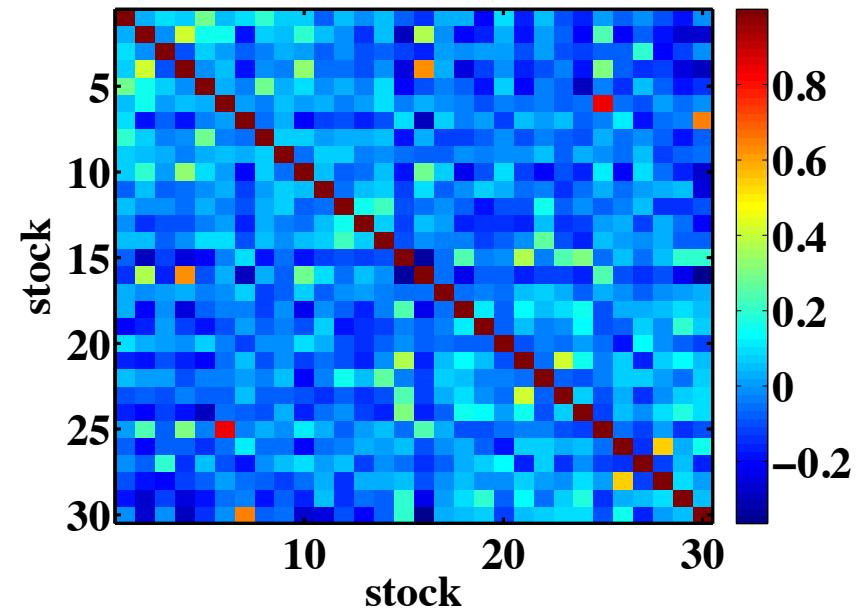
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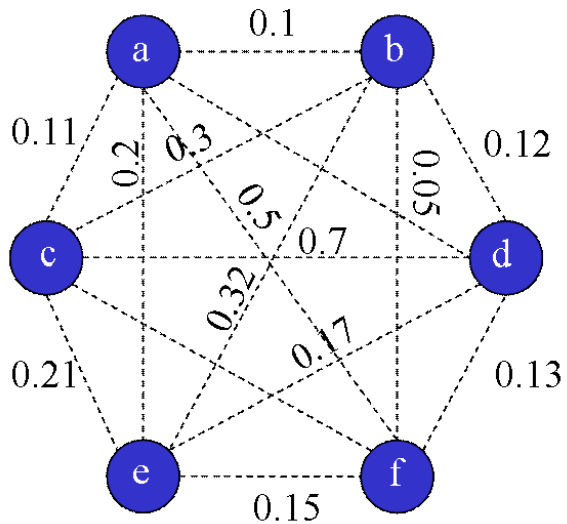
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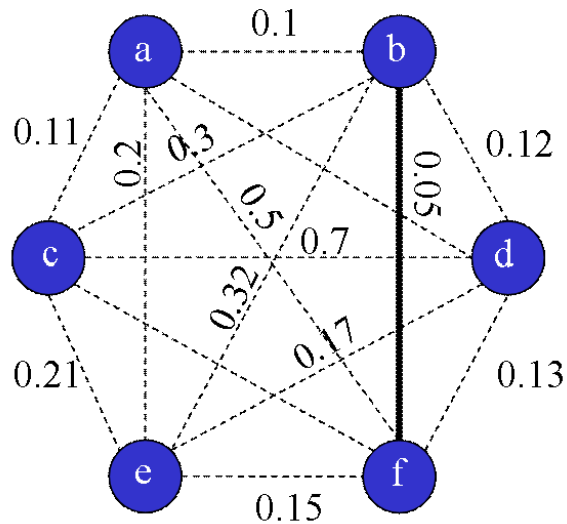
a b c d e f

a	0	0.1	0.11	0.4	0.2	0.5
b	0.1	0	0.3	0.12	0.32	0.05
c	0.11	0.3	0	0.7	0.21	0.5
d	0.4	0.12	0.7	0	0.17	0.13
e	0.2	0.32	0.21	0.17	0	0.15
f	0.5	0.05	0.5	0.13	0.15	0

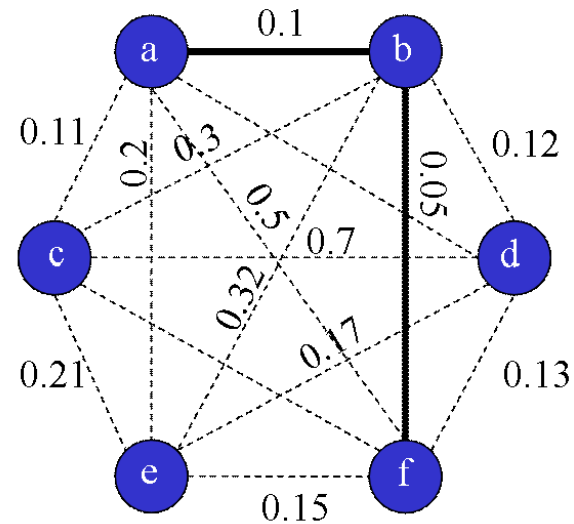
P_0



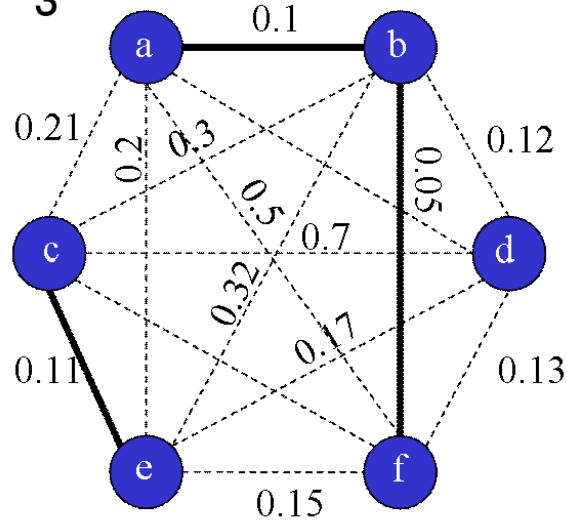
P_1



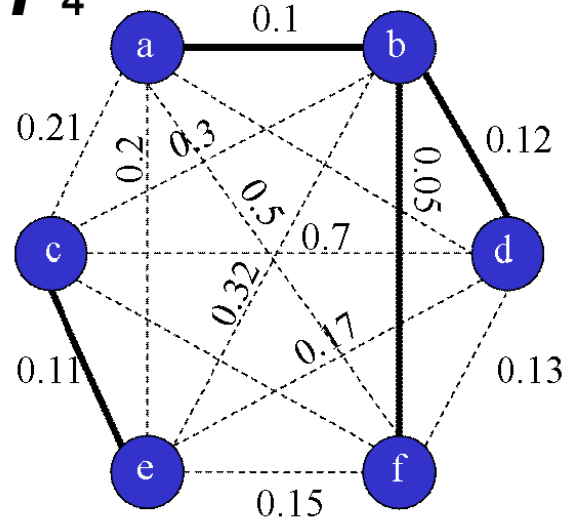
P_2



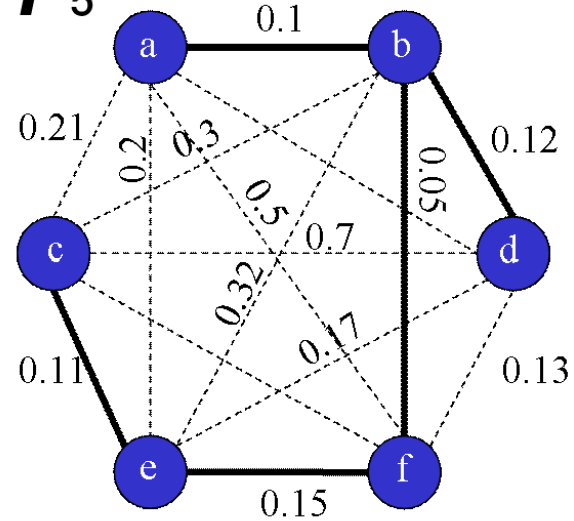
P_3



P_4



P_5



Stock Dependency Networks

1. Calculate partial correlation $PC(i, k | j) \quad j = 1, 2, \dots, N$

2. Correlation Influence

$$D(i, k | j) \equiv C(i, k) - PC(i, k | j)$$

3. Dependency Matrix $d(i | j) = \frac{1}{N-1} \sum_{k \neq j, i}^{N-1} D(i, k | j)$

4. Construct Planar Graph (PMFG, Tumminello *et al.*, PNAS 2005)

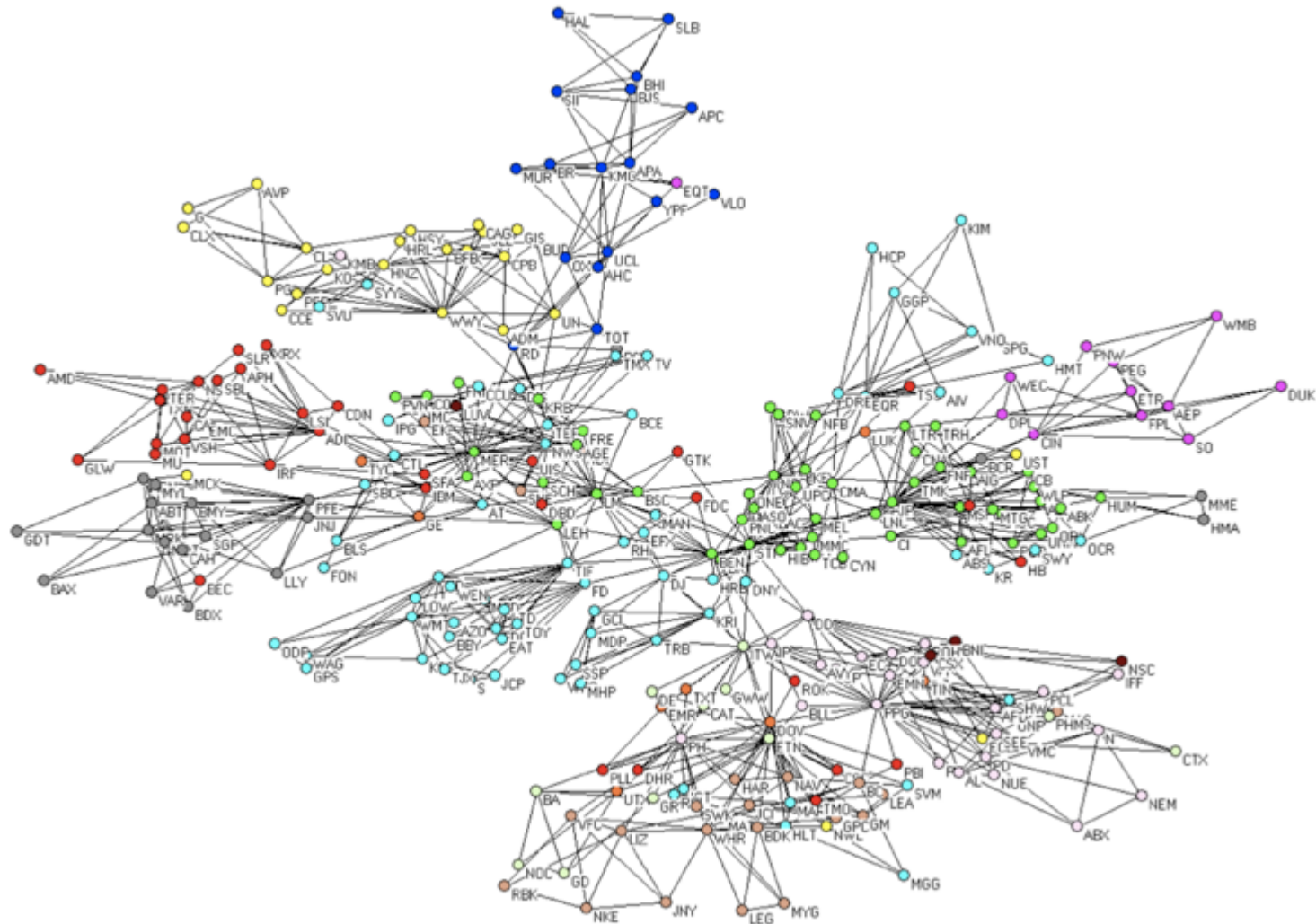
5. Influence and Relative Influence $R_u(s) = \frac{o(s) - i(s)}{o(s) + i(s)}$

Data

N = 300 **T = 748**

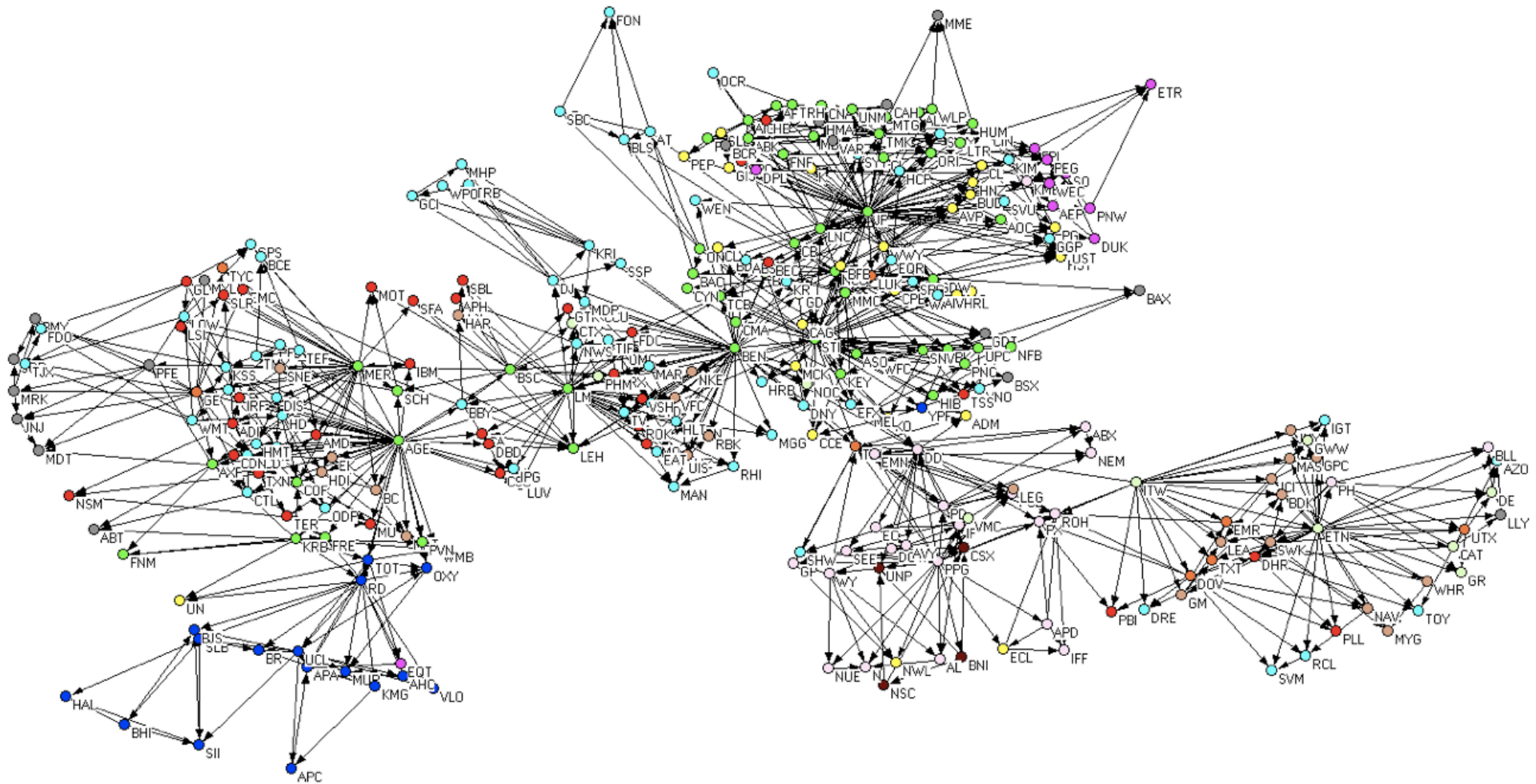
Index	Sector	# stocks
1	Basic Materials	24
2	Consumer Cyclical	22
3	Consumer Non Cyclical	25
4	Capital Goods	12
5	Conglomerates	8
6	Energy	17
7	Financial	53
8	Healthcare	19
9	Services	69
10	Technology	34
11	Transportation	5
12	Utilities	12

Stock Dependency Network: S&P Stocks



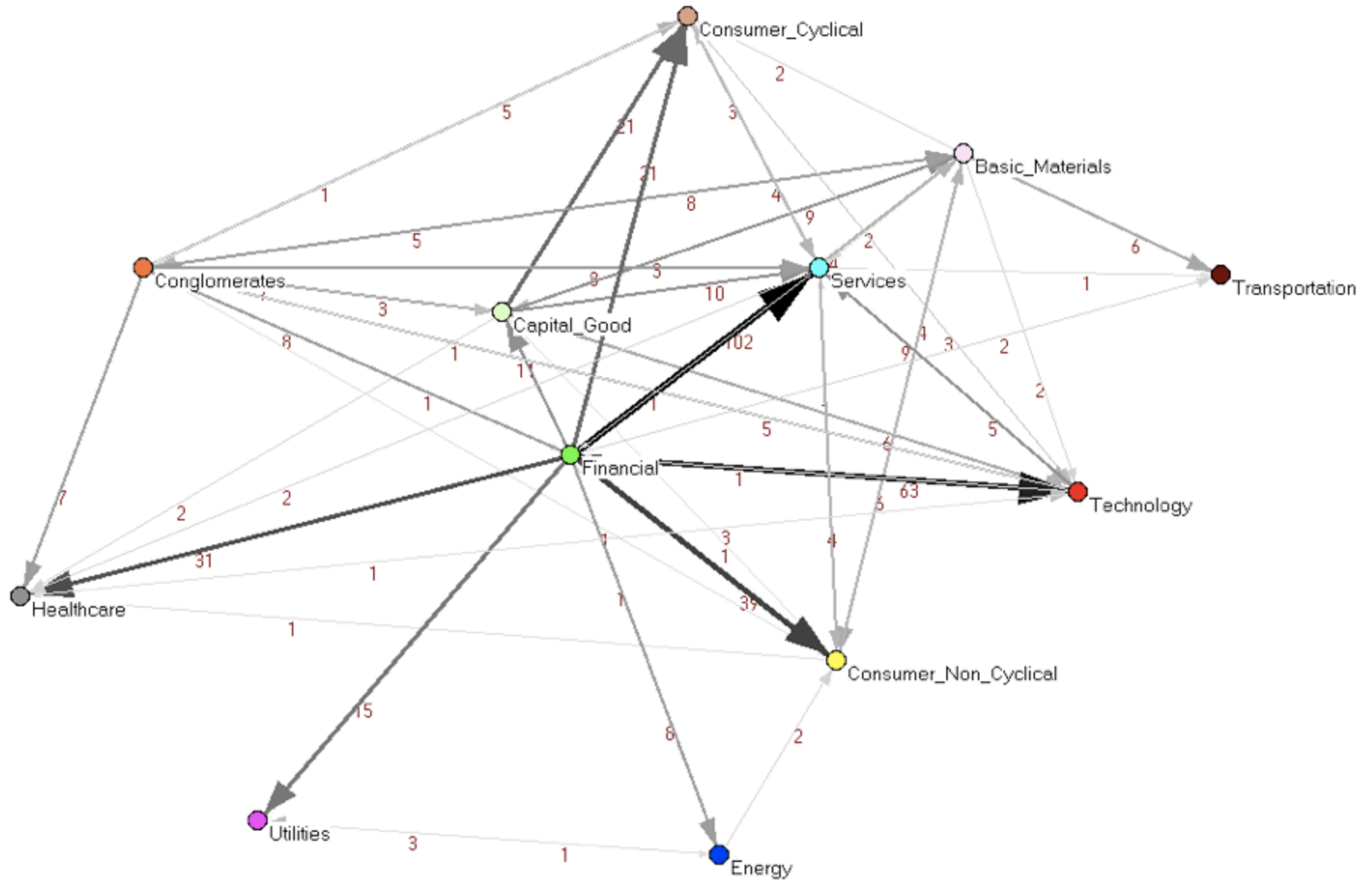
D.Y. Kenett, M. Tumminello, A. Madi, G. Gur-Gershgoren, R.N. Mantegna and E. Ben Jacob (2010), Dominating clasp of the financial sector revealed by partial correlation analysis of the stock market, PLoS ONE 5(12) e15032, doi:10.1371/journal.pone.0015032

Stock Dependency Network: S&P Stocks

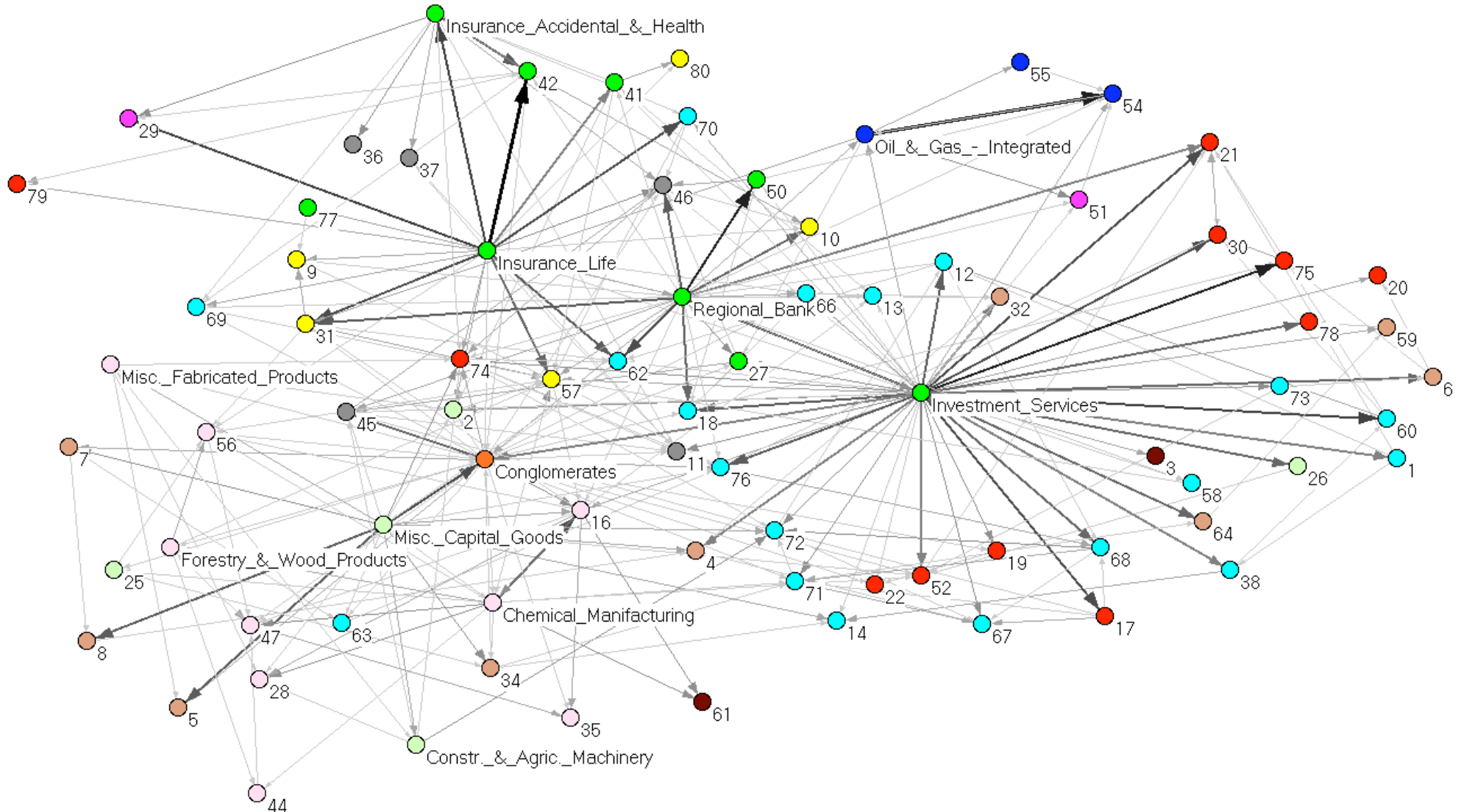


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Sector Dependency Network



Sector Dependency Network



Factor models

Factor models are simple and widespread model of multivariate time series

A general multifactor model for N variables $x_i(t)$ is

$$x_i(t) = \sum_{j=1}^K \gamma_i^{(j)} f_j(t) + \gamma_i^{(0)} \epsilon_i(t)$$

$\gamma_i^{(j)}$ is a constant describing the weight of factor j in explaining the dynamics of the variable $x_i(t)$.

The number of factors is K and they are described by the time series $f_j(t)$.

$\epsilon_i(t)$ is a (Gaussian) zero mean noise with unit variance

Factor models: examples

Multifactor models have been introduced to model a set of asset prices, generalizing CAPM

$$\mathbf{R}(t) = \mathbf{a} + \mathbf{B}\mathbf{f}(t) + \epsilon(t)$$

where now \mathbf{B} is a $(N \times K)$ matrix and $\mathbf{f}(t)$ is a $(K \times 1)$ vector of factors.

The factors can be selected either on a theoretical ground (e.g. interest rates for bonds, inflation, industrial production growth, oil price, etc.) or on a statistical ground (i.e. by applying factor analysis methods, etc.)

Examples of multifactor models are Arbitrage Pricing Theory (Ross 1976) and the Intertemporal CAPM (Merton 1973).

Factor models and Principal Component Analysis (PCA)

A factor is associated to each relevant eigenvalue-eigenvector

Number of relevant eigenvalues

i-th component of the h-th eigenvector of C

$$x_i(t) = \sum_{h=1}^K \gamma_i^{(h)} \sqrt{\lambda_h} f^{(h)}(t) + \sqrt{1 - \sum_{h=1}^K \gamma_i^{(h)2} \lambda_h} \varepsilon_i(t)$$

h-th eigenvalue

h-th factor

Idiosyncratic term

$f^{(h)}(t)$ for $h = 1, \dots, K$ and $\varepsilon_i(t)$ for $i = 1, \dots, n$

are i.i.d. random variables with mean 0 and variance 1

How many eigenvalues should be included ?

Random Matrix Theory

The idea is to **compare** the properties of an **empirical correlation matrix \mathbf{C}** with the null hypothesis of a **random matrix**.

$$Q = T/N \geq 1 \text{ fixed; } T \rightarrow \infty; N \rightarrow \infty$$

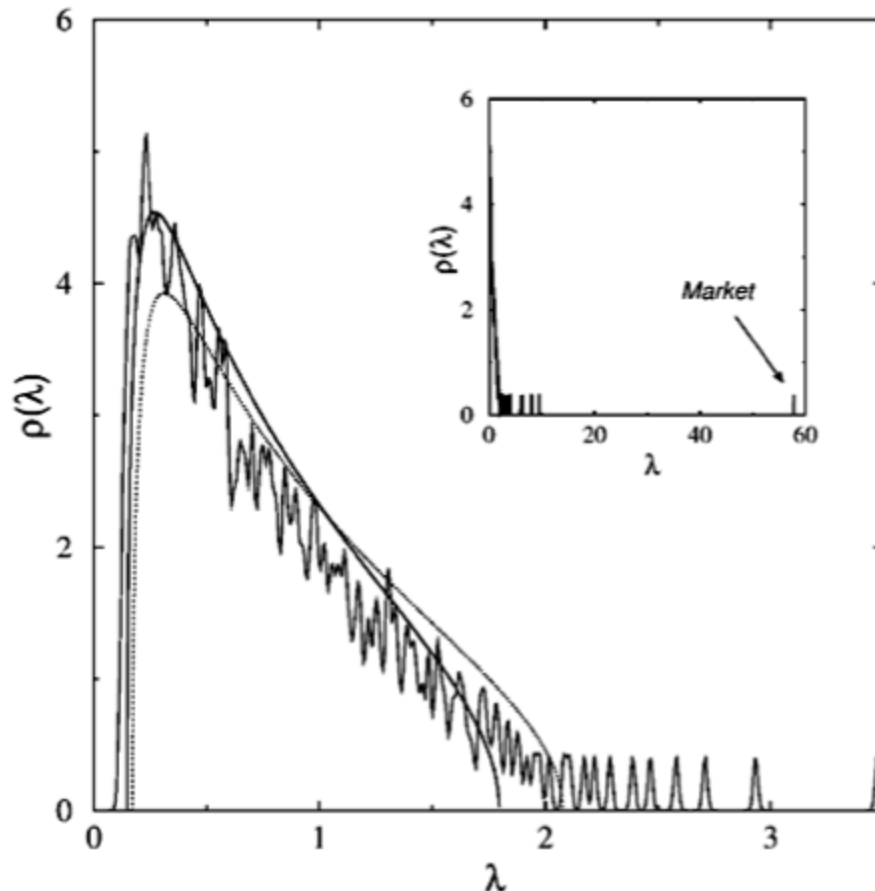
Density of eigenvalues of a Random Matrix

$$\rho(\lambda) = \frac{Q}{2\pi\sigma^2} \frac{\sqrt{(\lambda_{MAX} - \lambda)(\lambda - \lambda_{MIN})}}{\lambda}$$

$$\lambda_{MIN}^{MAX} = \sigma^2 \left(1 + 1/Q \pm 2\sqrt{1/Q}\right) \quad \text{For correlation matrices } \sigma^2 = 1$$

Random Matrix Theory

Random Matrix Theory helps to select the relevant eigenvalues



$N = 406$ assets of the
S & P 500 (1991 - 1996)

$Q = 3.22$

$\sigma^2 = 1 - \frac{1}{\lambda_1} \cong 0.85$ (dotted line)

best fit : $\sigma^2 = 0.74$ (solid line)

V. Plerou et al.

PRL 83, 1471 (1999)

L.Laloux et al,

PRL 83, 1468 (1999)

Theoretical Models

Simple Index

$$r_i = \gamma_i f + \sqrt{1 - \gamma_i^2} f \varepsilon_i, \quad i = 1, \dots, N,$$

$$\langle r_i f \rangle = \gamma_i \langle f^2 \rangle = \gamma_i,$$

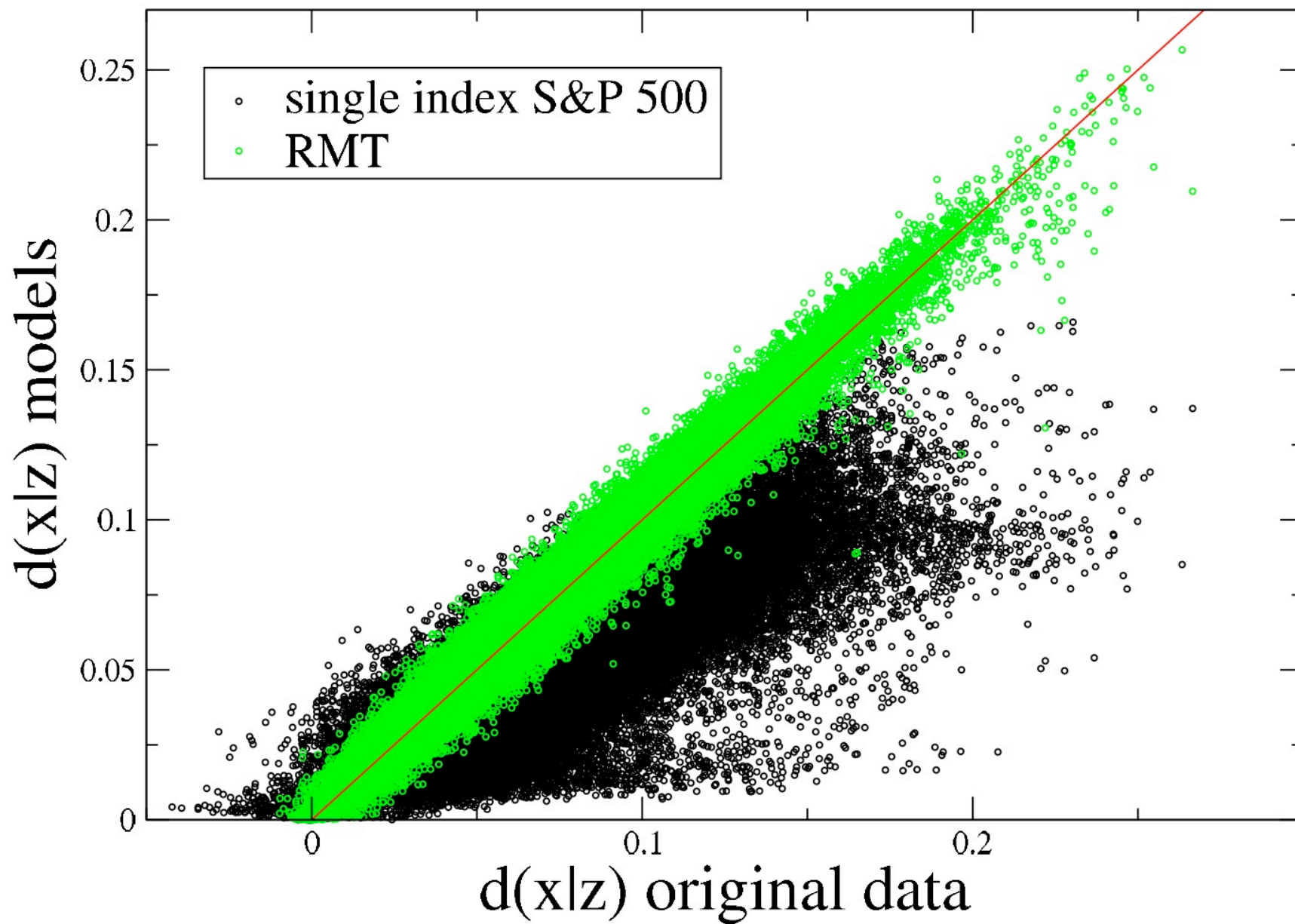
$$\rho_{i,j}(SI) = \langle r_i r_j \rangle = \gamma_i \gamma_j$$

RMT

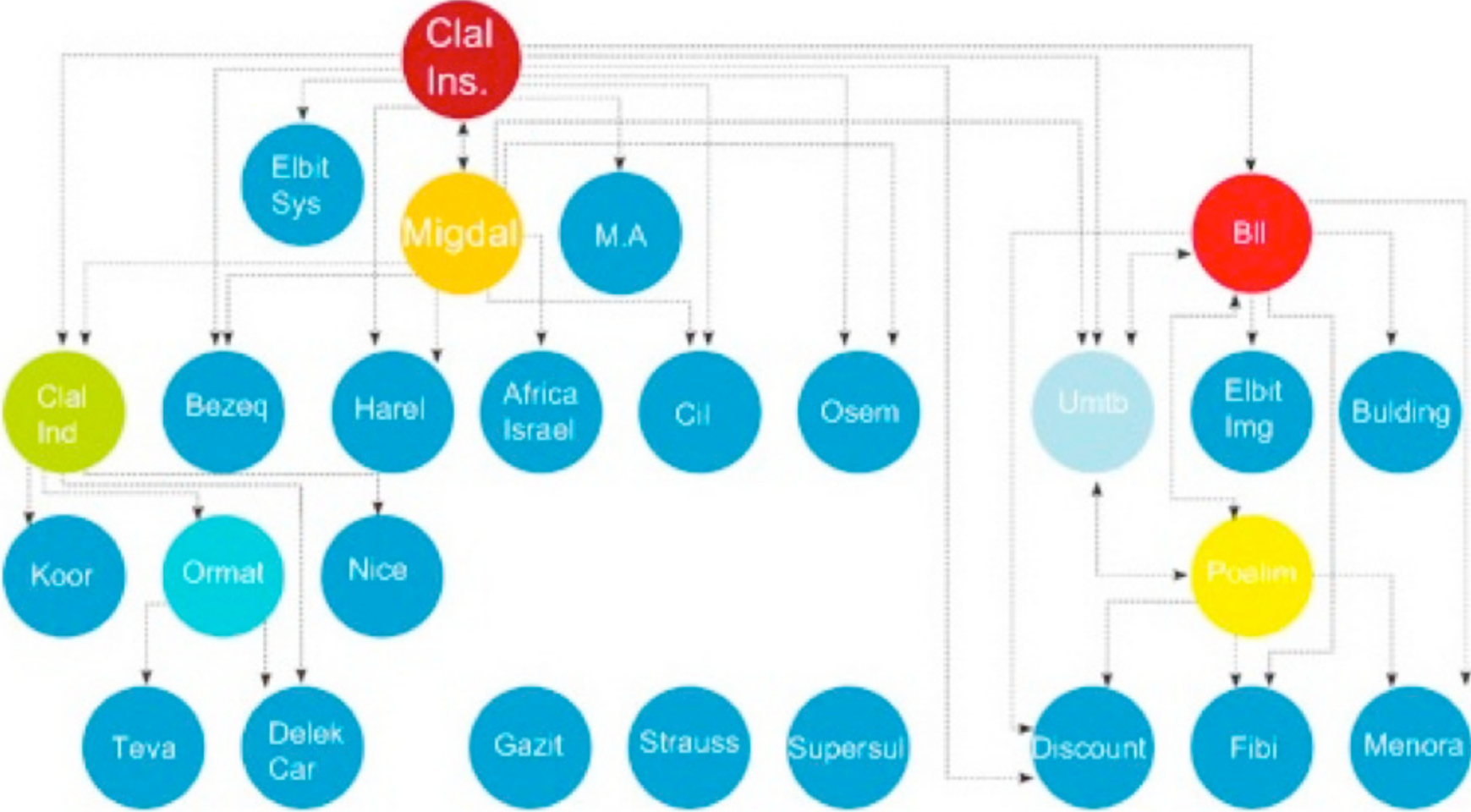
$$r_i = \sum_{h=1}^K \gamma_{i,h} \sqrt{\lambda_h} f_h + \sqrt{1 - \sum_{h=1}^k \gamma_{i,h}^2 \lambda_h} \varepsilon_i \quad i = 1, \dots, N,$$

$$\lambda_{\max} = \left(1 - \frac{\lambda_1}{N}\right) \left(1 + \frac{N}{T} + 2\sqrt{\frac{N}{T}}\right)$$

$$\rho_{i,j}(RMT) = \langle r_i r_j \rangle = \sum_{h=1}^K \gamma_{i,h} \gamma_{j,h} \lambda_h$$



Case study - Tel-Aviv market

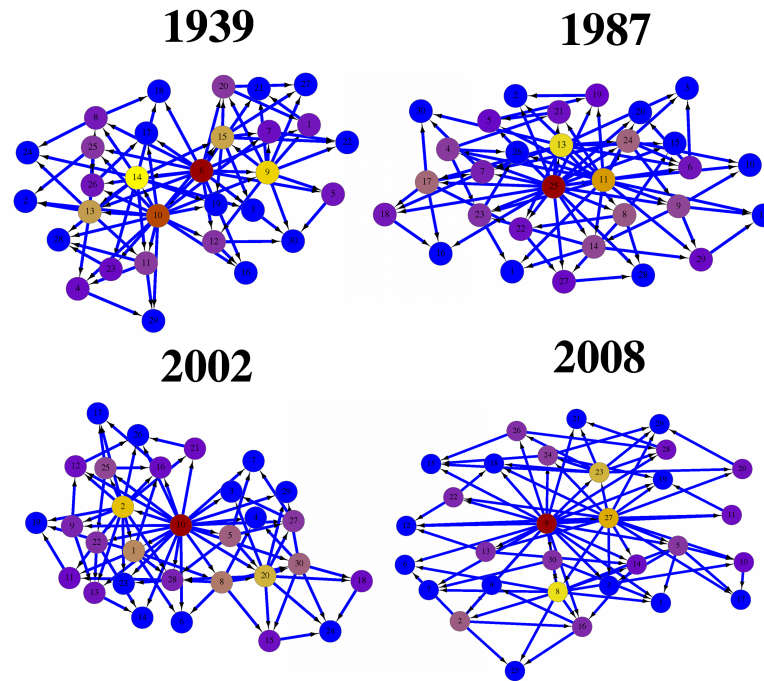
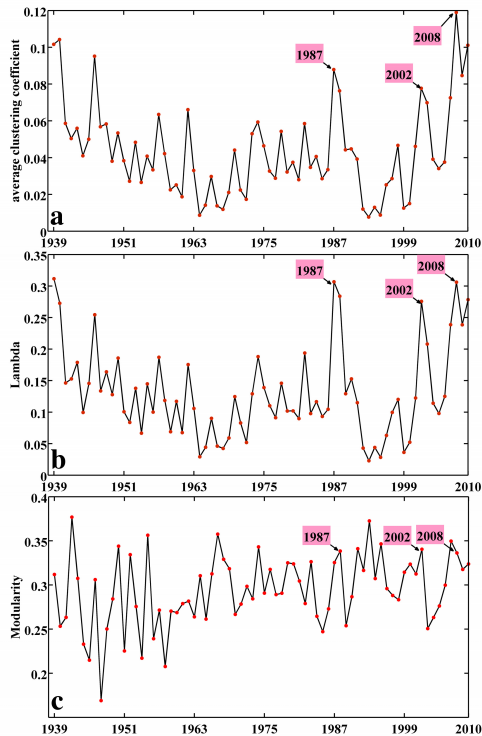
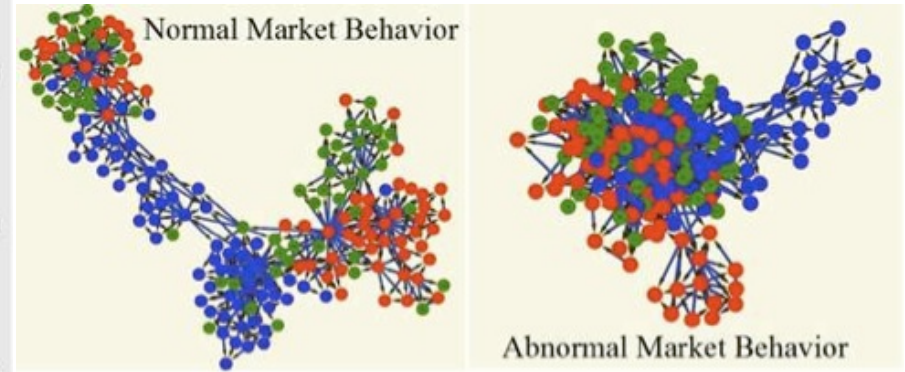
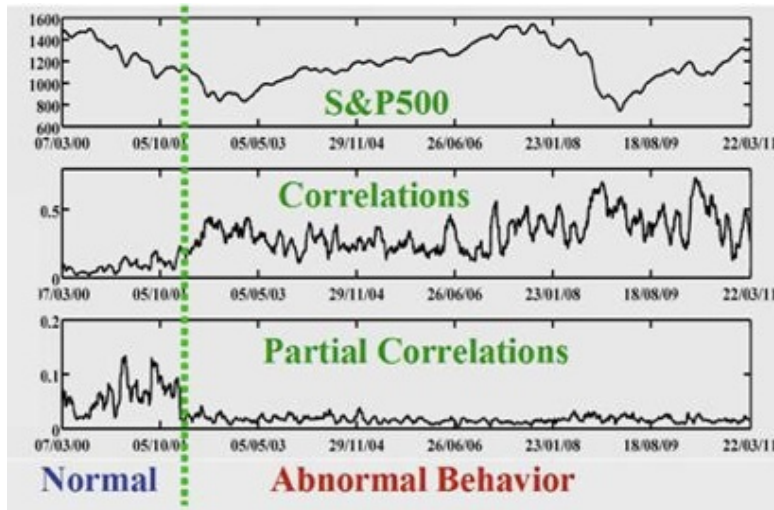


No Influence

Influence

Strong Influence

Market states

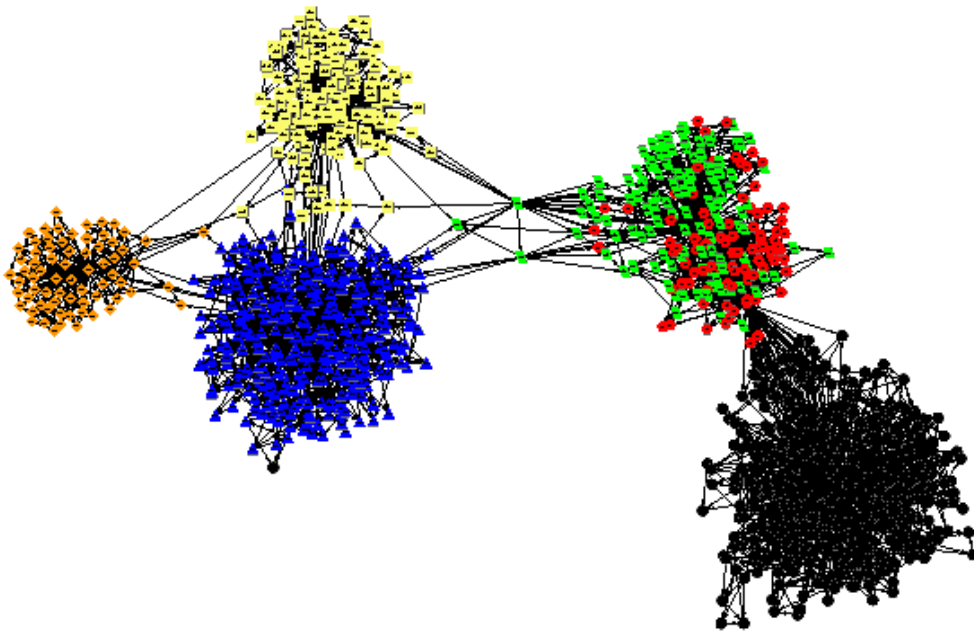


Dynamics analysis of Dependency networks

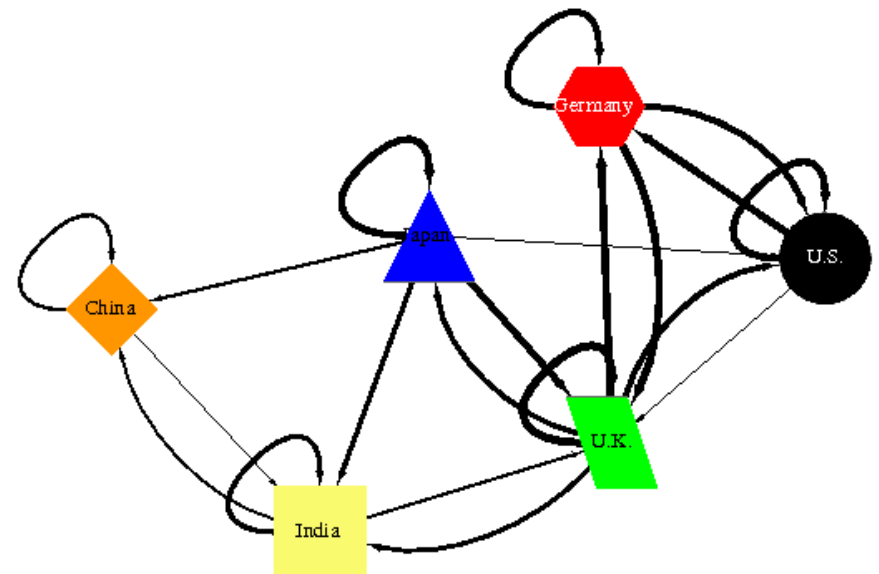
Interdependencies in the global financial village

Network analysis of influence and dependencies between Companies/Countries

Stock dependency network



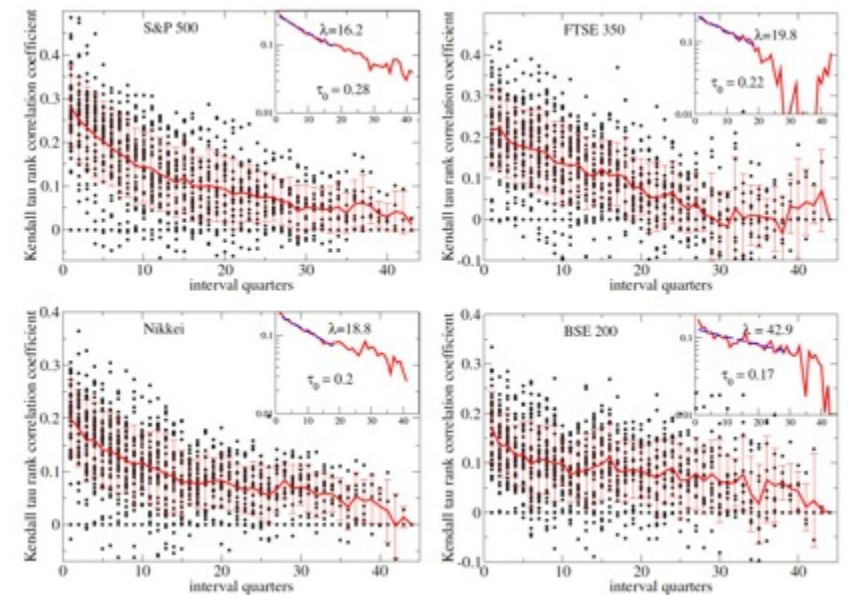
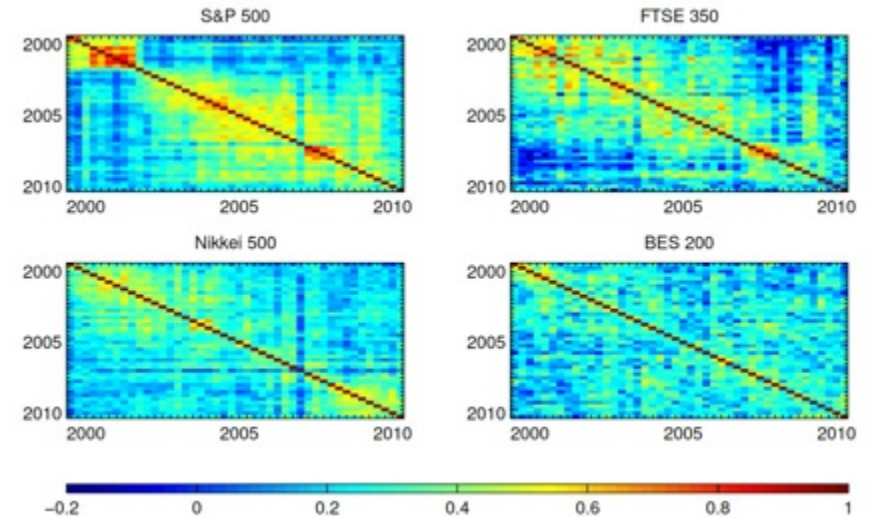
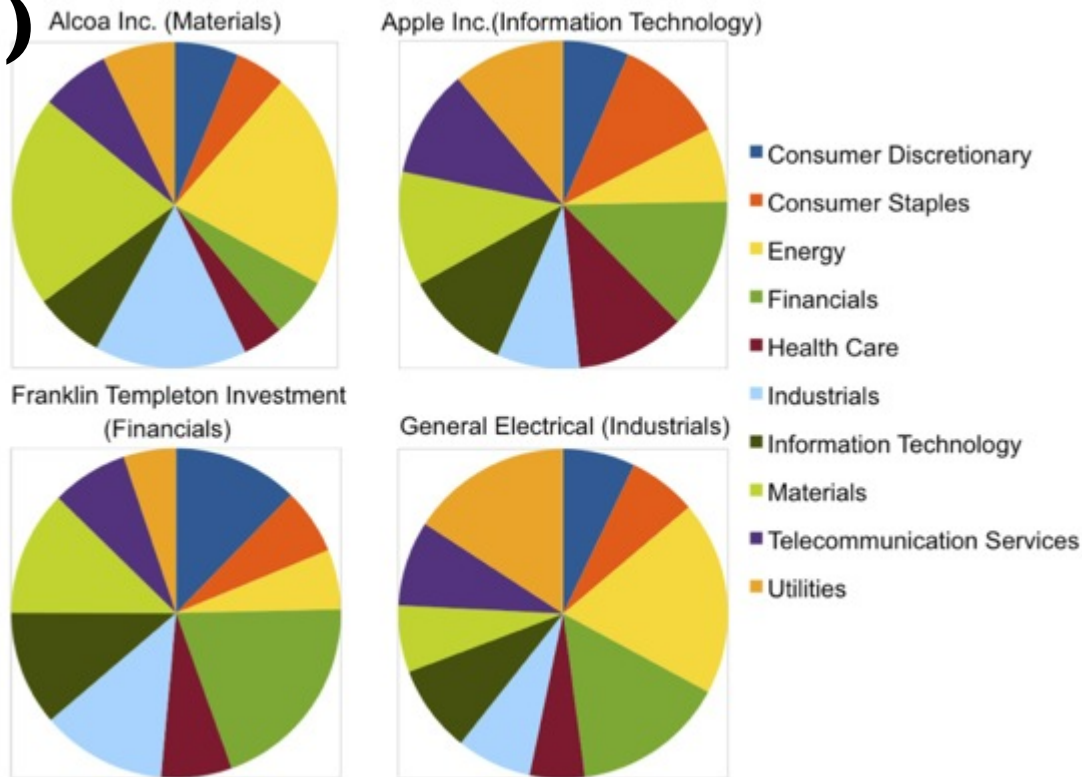
Country dependency network



Investigating market structure

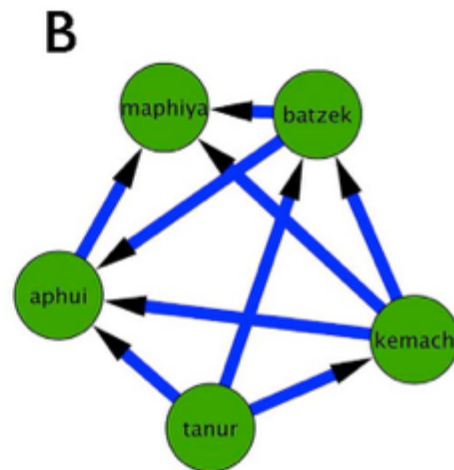
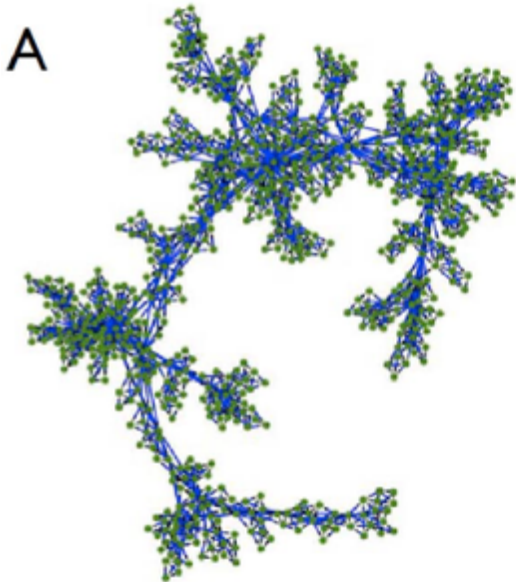
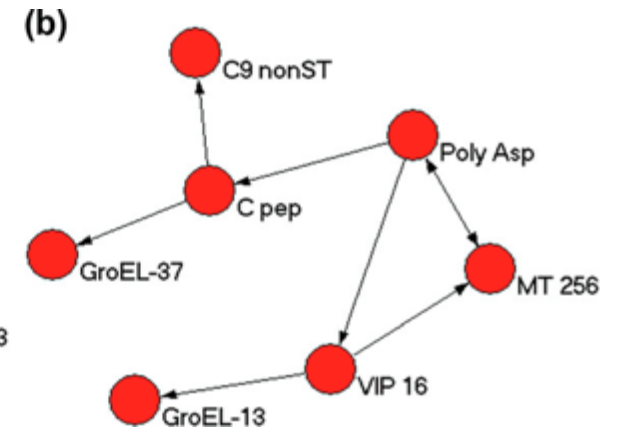
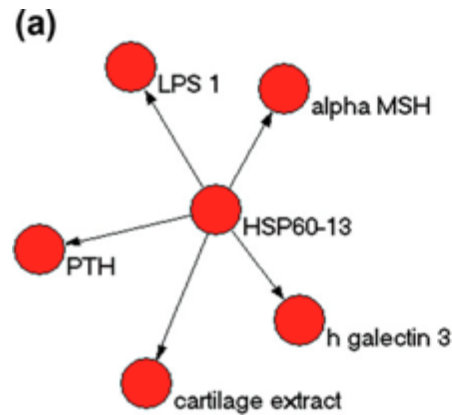
2)

1)



Application to other systems

Immune system Dependency network



Semantic Dependency network

Outline

(1) Introduction to network science

- Terminology
- Network properties
- Matrix representation

(2) Correlation based networks

- Estimating correlations from
- Partial correlations
- Dependency network
- Node influence
- Applications in financial markets
- Applications in other systems

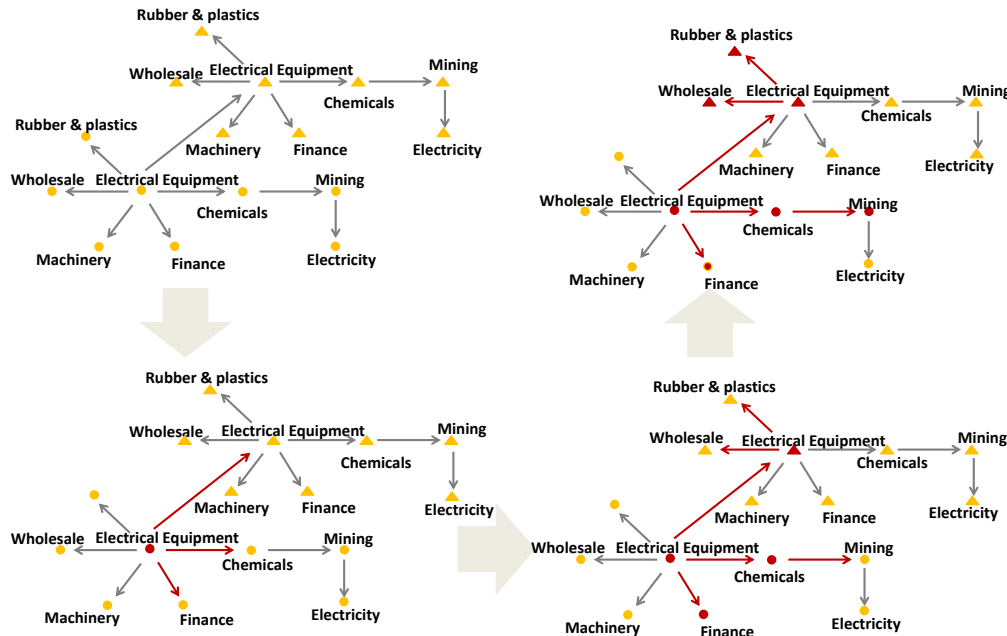
(3) Node influence

- I. Cascading failures in industry networks
- II. Overlapping communities in networks
- III. Failure and recovery in networks
- IV. Evolution of networks
- V. Cascading failures in the financial system
- VI. Interdependent networks

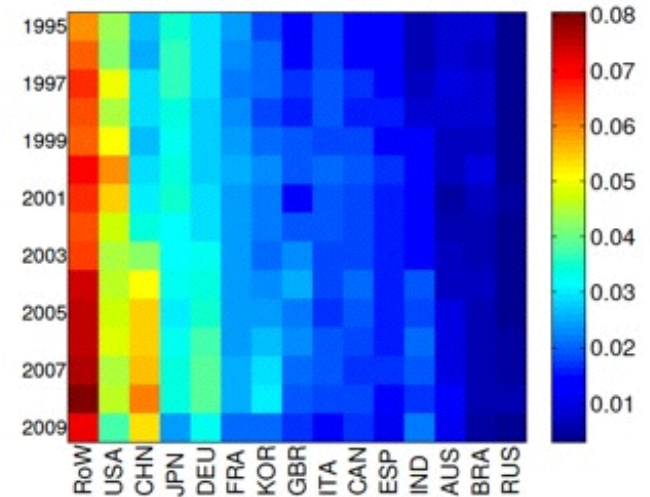
(4) Discussion

I. Cascading failures in industry networks

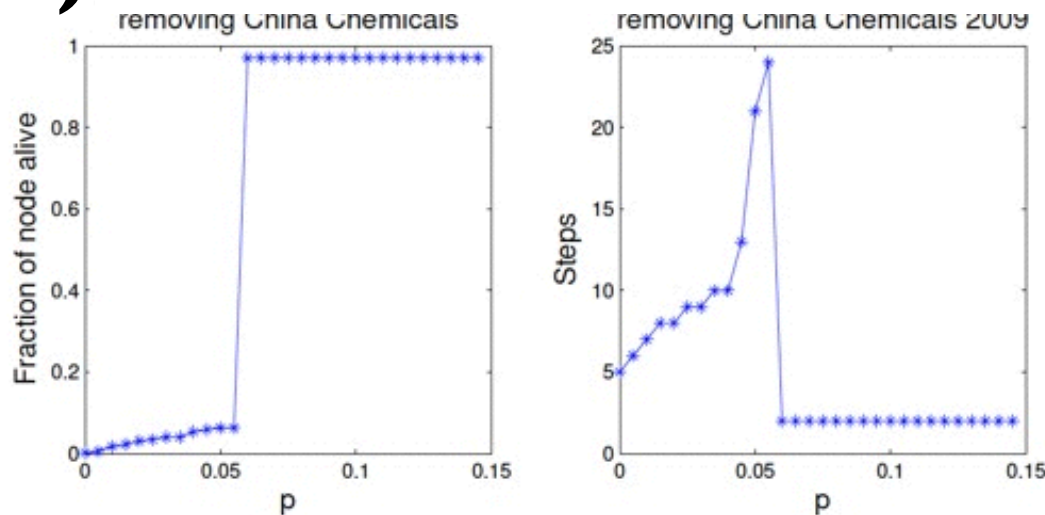
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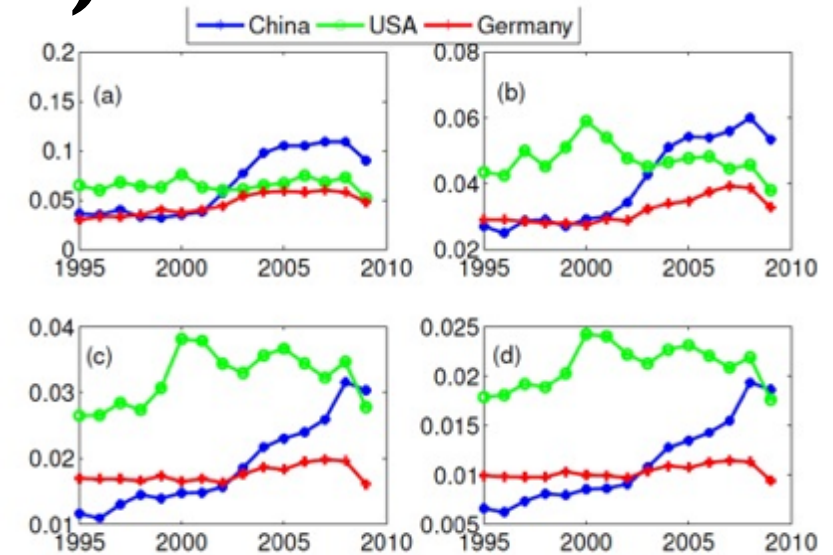
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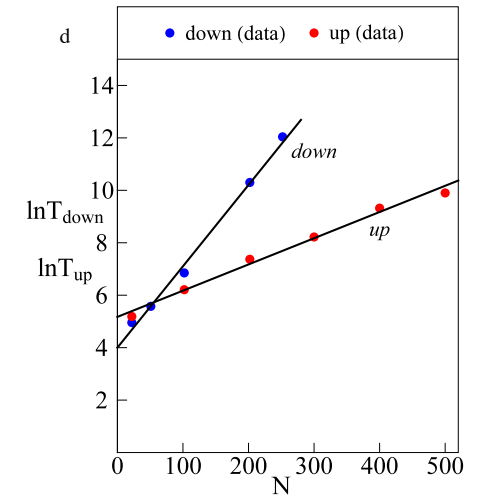
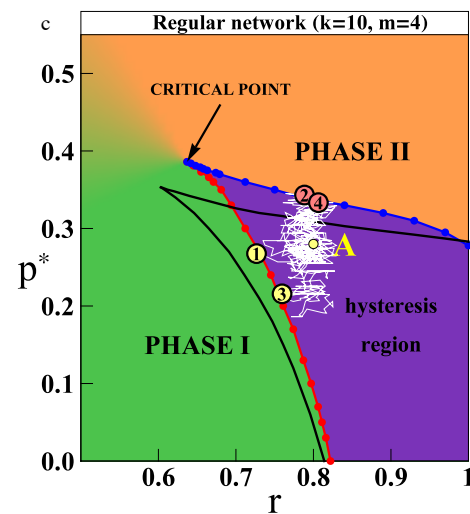
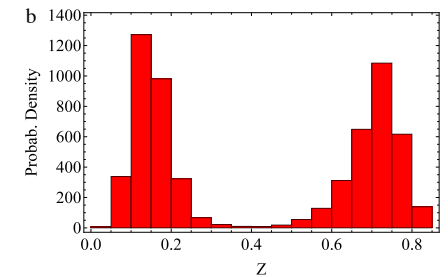
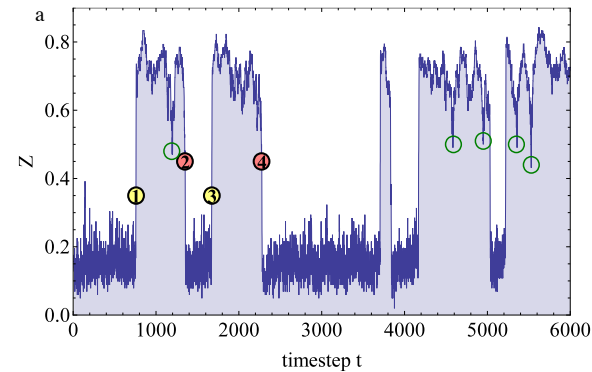


4)



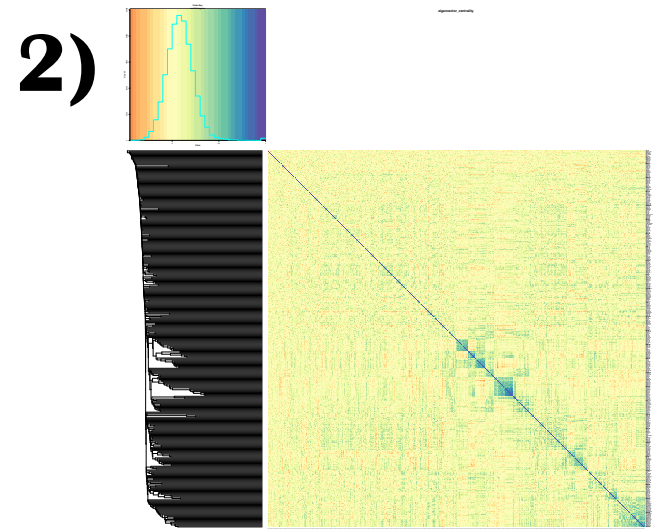
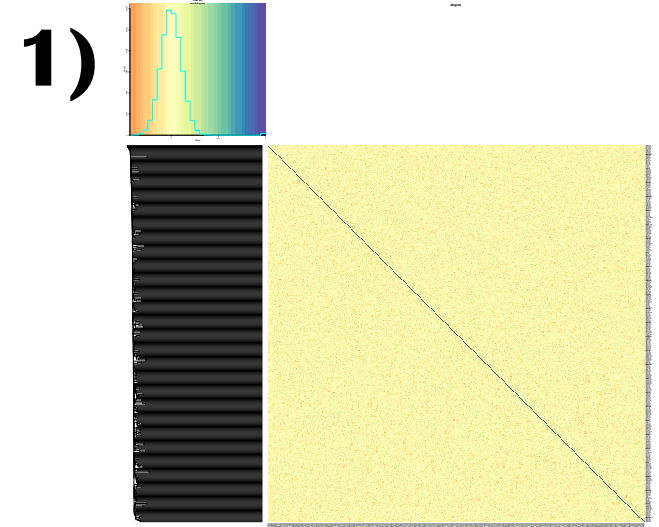
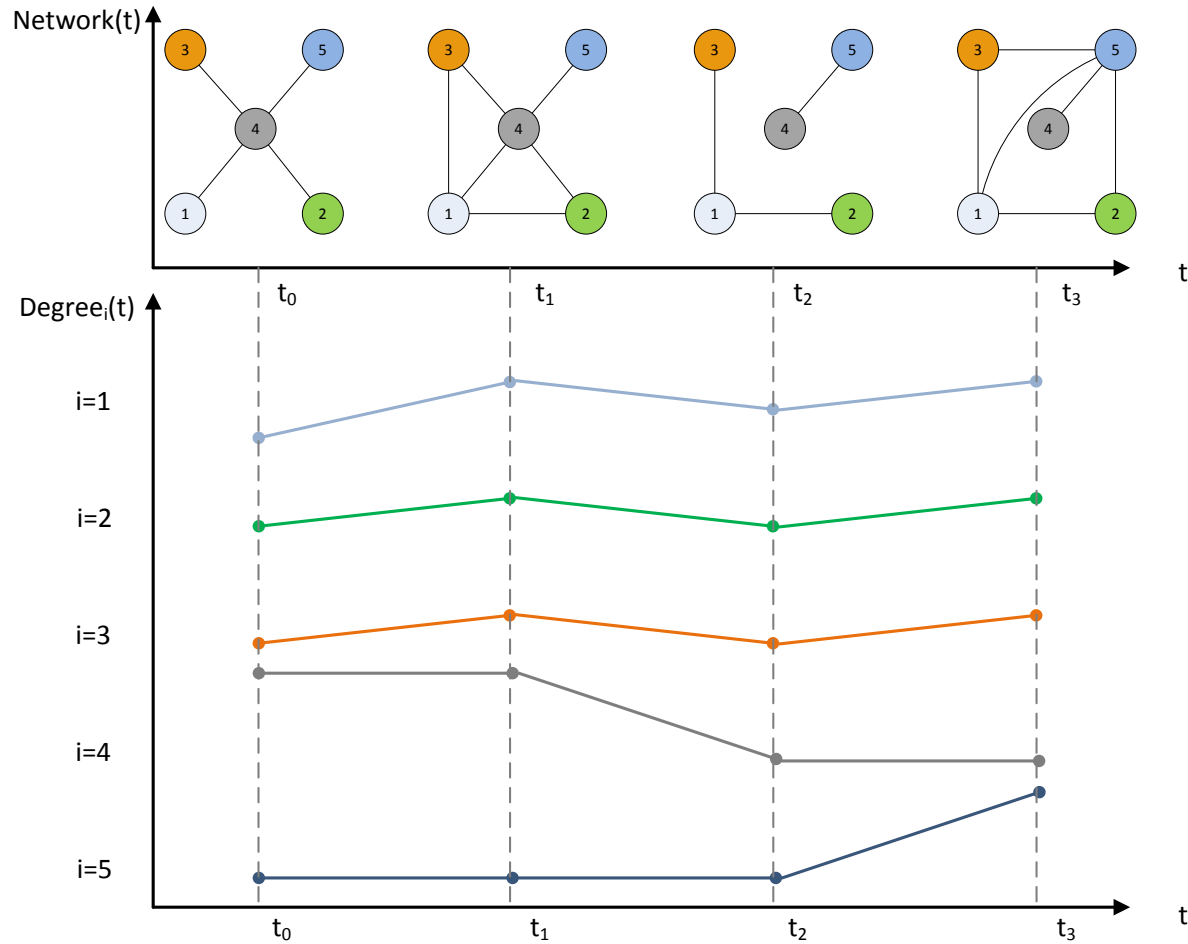
Wei Li, Dror Y. Kenett, Kazuko Yamasaki, H. Eugene Stanley, Shlomo Havlin (preprint), Ranking the economic importance of countries and industries

III. Failure and recovery in networks



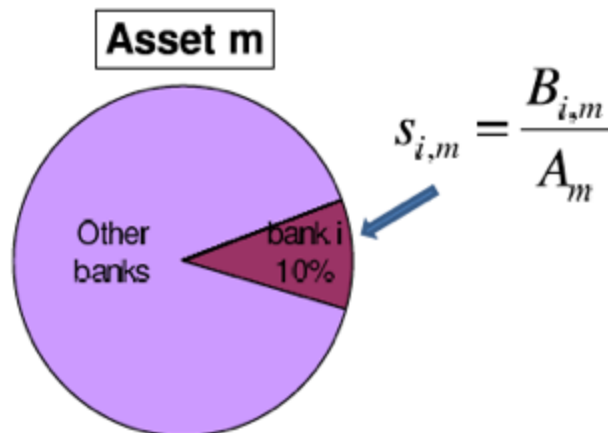
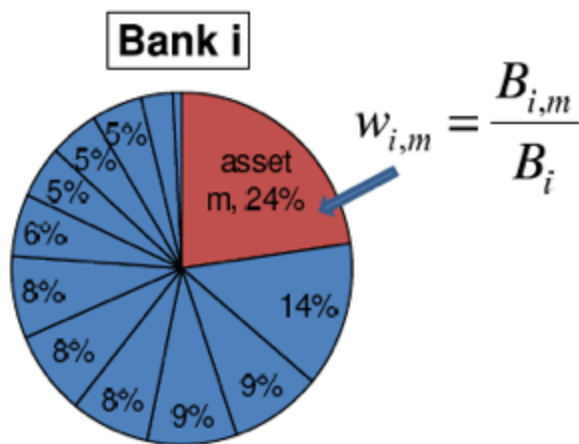
Antonio Majdandzic, Boris Podobnik, Sergey Buldyrev, Dror Y. Kenett, Shlomo Havlin, and H. Eugene Stanley (2014), Spontaneous recovery in dynamical networks, Nature Physics 10, 34-38.

IV. Evolution of networks

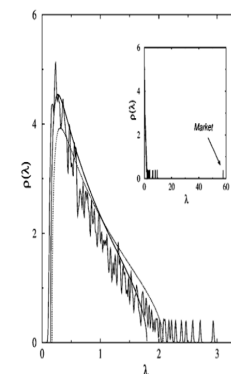
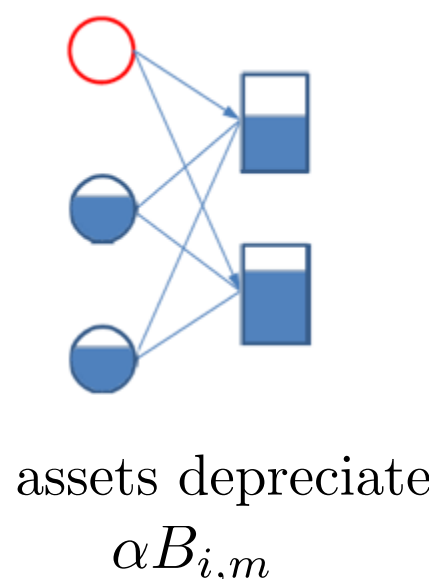
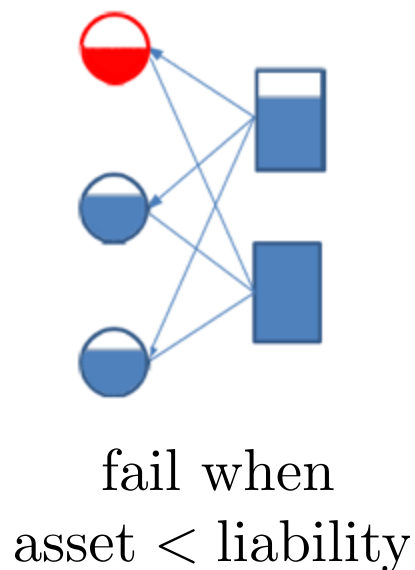
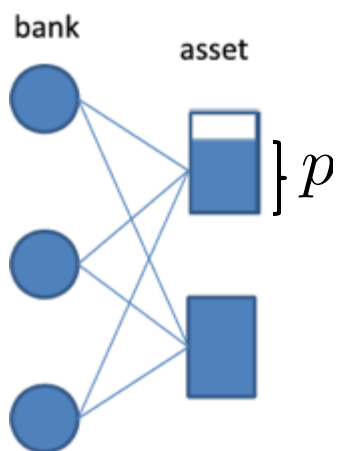


V. Cascading failures in the financial system

Bipartite Model

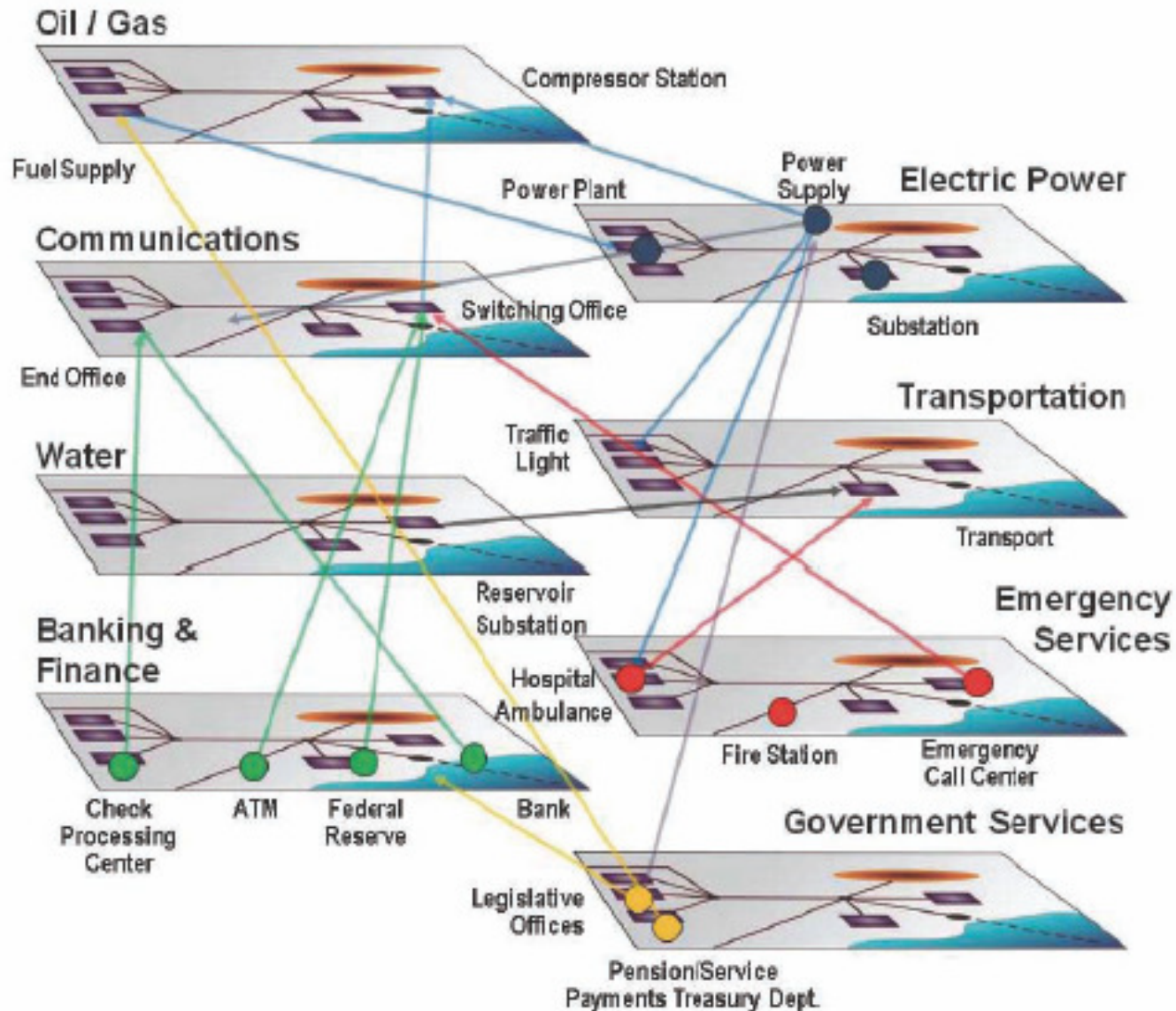


B_i : Total asset of bank i .
 $B_{i,m}$: The amount of asset m that bank i owns.
 A_m : Total market value of asset m .



1-p: initial shock to an asset
 α : liquidity parameter
 describes market's reaction to bank failure

VI. Interdependent networks



Buldyrev, S. V., Parshani, R., Paul, G., Stanley, H. E., & Havlin, S. (2010). Catastrophic cascade of failures in interdependent networks. *Nature*, 464(7291), 1025-1028.

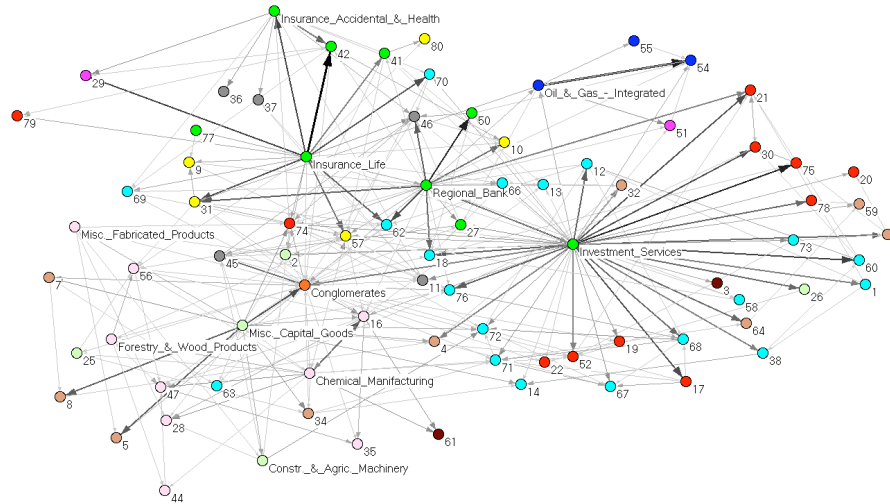
Summary

- **Dependency Networks**
- **Node influence**
- **Network in finance and economics**
- **Topology of networks**
- **Dynamics in networks and of networks**
- **Interdependent networks**
- **Cascading failures and targeted attacks**
- **Recovery in networks**

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11. Dror Y. Kenett, Xuqing Huang, Irena Vodenska, Shlomo Havlin, and H. Eugene Stanley (2014) Analysis: Applications for financial markets, arXiv:1402.1405

Thank You



Questions?

Email: drorkenett@gmail.com